


A mostly complete chart of Neural Networks

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-  Backfed Input Cell
-  Input Cell
-  Noisy Input Cell
-  Hidden Cell
-  Probabilistic Hidden Cell
-  Spiking Hidden Cell
-  Output Cell
-  Match Input Output Cell
-  Recurrent Cell
-  Memory Cell
-  Different Memory Cell
-  Kernel
-  Convolution or Pool

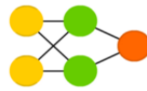
Deep Feed Forward (DFF)



Perceptron (P)



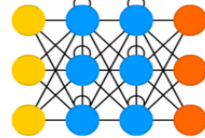
Feed Forward (FF)



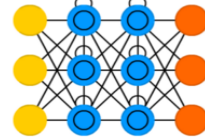
Radial Basis Network (RBF)



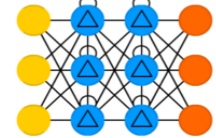
Recurrent Neural Network (RNN)



Long / Short Term Memory (LSTM)



Gated Recurrent Unit (GRU)



Auto Encoder (AE)



Variational AE (VAE)



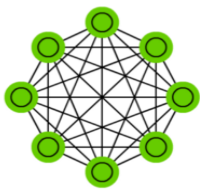
Denosing AE (DAE)



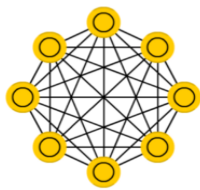
Sparse AE (SAE)



Markov Chain (MC)



Hopfield Network (HN)



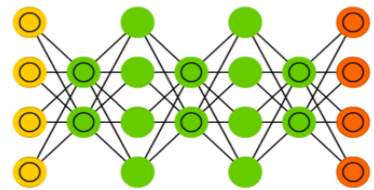
Boltzmann Machine (BM)



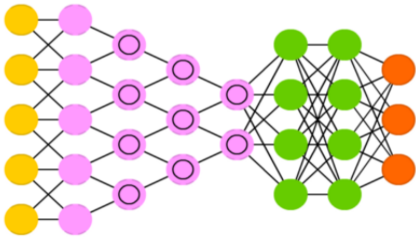
Restricted BM (RBM)



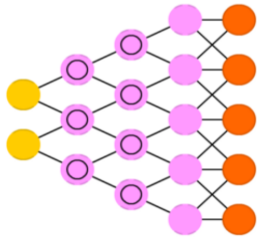
Deep Belief Network (DBN)



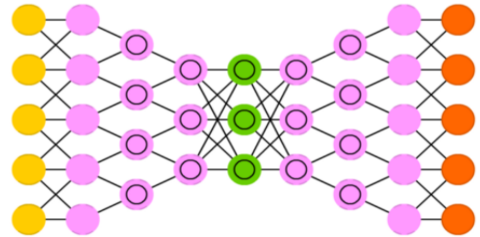
Deep Convolutional Network (DCN)



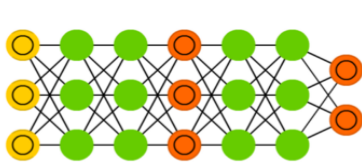
Deconvolutional Network (DN)



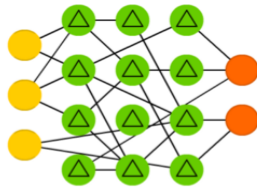
Deep Convolutional Inverse Graphics Network (DCIGN)



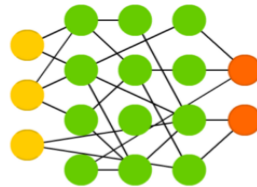
Generative Adversarial Network (GAN)



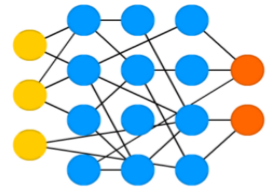
Liquid State Machine (LSM)



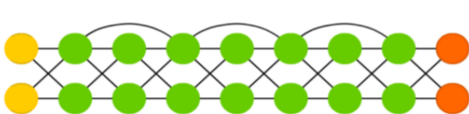
Extreme Learning Machine (ELM)



Echo State Network (ESN)



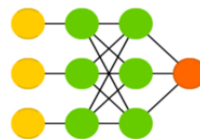
Deep Residual Network (DRN)



Kohonen Network (KN)



Support Vector Machine (SVM)

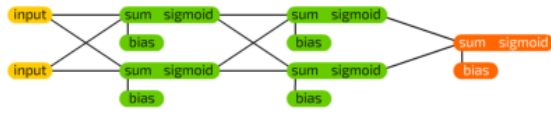


Neural Turing Machine (NTM)

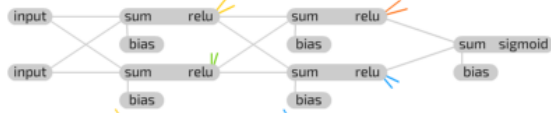
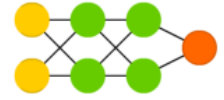


An informative chart to build Neural Network Graphs

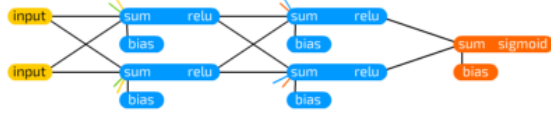
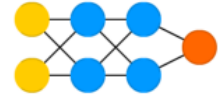
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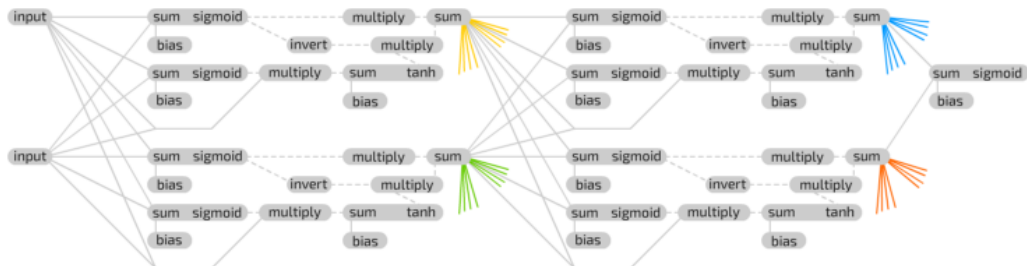
Deep Feed Forward Example



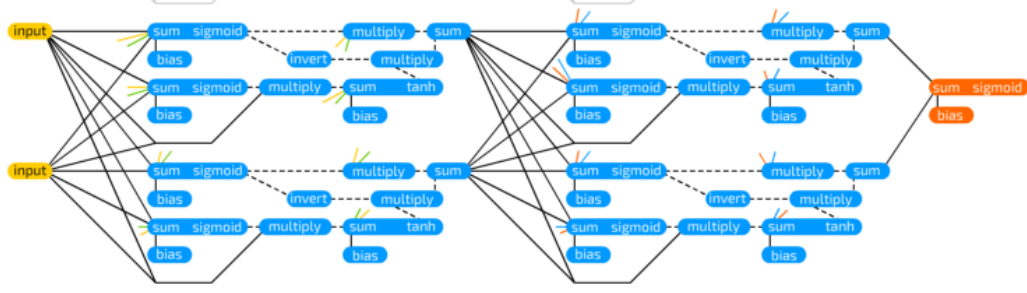
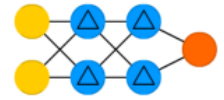
Deep Recurrent Example
(previous iteration)



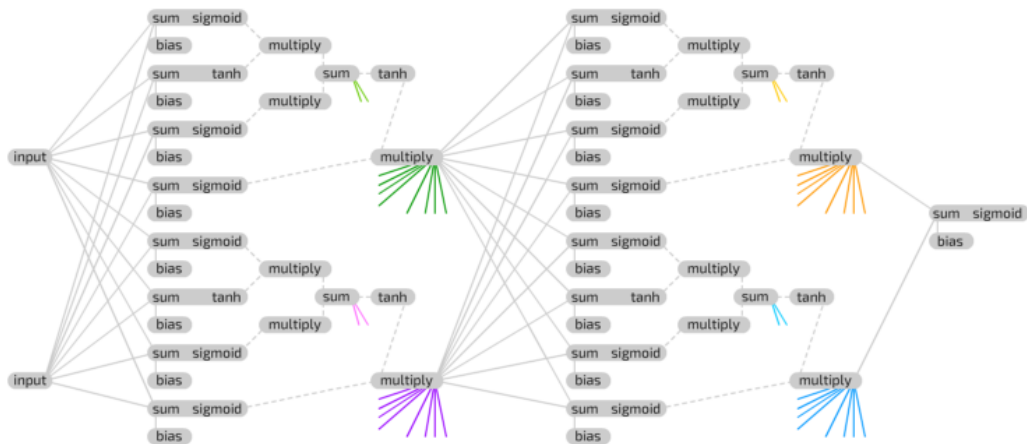
Deep Recurrent Example



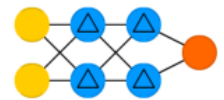
Deep GRU Example
(previous iteration)



Deep GRU Example



Deep LSTM Example
(previous iteration)



Deep LSTM Example

Linear Vector Spaces:

Definition: A linear vector space, X is a set of elements (vectors) defined over a scalar field, F , that satisfies the following conditions:

- 1) if $x \in X$ and $y \in X$ then $x+y \in X$.
- 2) $x+y = y+x$
- 3) $(x+y)+z = x+(y+z)$
- 4) There is a unique vector $\theta \in X$, such that $x+\theta = x$ for all $x \in X$.
- 5) For each vector $x \in X$ there is a unique vector in X , to be called $(-x)$, such that $x+(-x) = \theta$.
- 6) multiplication, for all scalars $a \in F$, and all vectors $x \in X$,
- 7) For any $x \in X$, $1x = x$ (for scalar 1).
- 8) For any two scalars $a \in F$ and $b \in F$ and any $x \in X$, $a(bx) = (ab)x$.
- 9) $(a+b)x = ax + bx$.
- 10) $a(x+y) = ax + ay$.

Linear Independence: Consider n vectors $\{x_1, x_2, \dots, x_n\}$. If there exists n scalars a_1, a_2, \dots, a_n , at least one of which is nonzero, such that $a_1x_1 + a_2x_2 + \dots + a_nx_n = \theta$, then the $\{x_i\}$ are linearly dependent.

Spanning a Space:

Let X be a linear vector space and let $\{u_1, u_2, \dots, u_n\}$ be a subset of vectors in X . This subset spans X if and only if for every vector $x \in X$ there exist scalars x_1, x_2, \dots, x_n such that $x = x_1u_1 + x_2u_2 + \dots + x_nu_n$.

Inner Product: (x, y) for any scalar function of x and y .

1. $(x, y) = (y, x)$
2. $(x, ay_1 + by_2) = a(x, y_1) + b(x, y_2)$
3. $(x, x) \geq 0$, where equality holds iff x is the zero vector.

Norm: A scalar function $\|x\|$ is called a norm if it satisfies:

1. $\|x\| \geq 0$
2. $\|x\| = 0$ if and only if $x = \theta$.
3. $\|ax\| = |a|\|x\|$
4. $\|x + y\| \leq \|x\| + \|y\|$

Angle: The angle θ bet. 2 vectors x and y is defined by $\cos \theta = \frac{(x, y)}{\|x\| \|y\|}$

Orthogonality: 2 vectors $x, y \in X$ are said to be orthogonal if $(x, y) = 0$.

Gram Schmidt Orthogonalization:

Assume that we have n independent vectors y_1, y_2, \dots, y_n . From these vectors we will obtain n orthogonal vectors v_1, v_2, \dots, v_n .

$$v_1 = y_1, \quad v_k = y_k - \sum_{i=1}^{k-1} \frac{(y_k, v_i)}{(v_i, v_i)} v_i,$$

where $\frac{(v_i, y_k)}{(v_i, v_i)} v_i$ is the projection of y_k on v_i

Vector Expansions:

$$x = \sum_{i=1}^n x_i v_i = x_1 v_1 + x_2 v_2 + \dots + x_n v_n,$$

for orthogonal vectors, $x_j = \frac{(v_j, x)}{(v_j, v_j)}$

Reciprocal Basis Vectors:

$$(r_i, v_j) = \begin{cases} 0 & i \neq j \\ 1 & i = j \end{cases}, \quad x_j = (r_j, x)$$

To compute the reciprocal basis vectors: set $B = [v_1 \ v_2 \ \dots \ v_n]$,

$R = [r_1 \ r_2 \ \dots \ r_n]$, $R^T = B^{-1}$ In matrix form: $x^v = B^{-1} x^s$

Transformations:

A transformation consists of three parts:

domain: $X = \{x_i\}$, range: $Y = \{y_i\}$, and a rule relating each $x_i \in X$ to an element $y_i \in Y$.

Linear Transformations: transformation A is linear if:

1. for all $x_1, x_2 \in X$, $A(x_1 + x_2) = A(x_1) + A(x_2)$
2. for all $x \in X$, $a \in R$, $A(ax) = aA(x)$

Matrix Representations:

Let $\{v_1, v_2, \dots, v_n\}$ be a basis for vector space X , and let $\{u_1, u_2, \dots, u_n\}$ be a basis for vector space Y . Let A be a linear transformation with domain X and range Y : $A(x) = y$

The coefficients of the matrix representation are obtained from

$$A(v_j) = \sum_{i=1}^m a_{ij} u_i$$

Change of Basis: $B_t = [t_1 \ t_2 \ \dots \ t_n]$, $B_w = [w_1 \ w_2 \ \dots \ w_n]$
 $A' = [B_w^{-1} A B_t]$

Eigenvalues & Eigenvectors: $Az = \lambda z$, $|[A - \lambda I]| = 0$

Diagonalization: $B = [z_1 \ z_2 \ \dots \ z_n]$,

where $\{z_1, z_2, \dots, z_n\}$ are the eigenvectors of a square matrix A ,
 $[B^{-1} A B] = \text{diag}([\lambda_1 \ \lambda_2 \ \dots \ \lambda_n])$

Perceptron Architecture:

$$a = \text{hardlim}(Wp + b), \quad W = [{}_1w^T \ {}_2w^T \ \dots \ {}_sw^T]^T, \\ a_i = \text{hardlim}(n_i) = \text{hardlim}({}_i w^T p + b_i)$$

Decision Boundary: ${}_i w^T p + b_i = 0$

The decision boundary is always orthogonal to the weight vector. Single-layer perceptrons can only classify linearly separable vectors.

Perceptron Learning Rule

$$W^{new} = W^{old} + ep^T, \quad b^{new} = b^{old} + e, \\ \text{where } e = t - a$$

Hebb's Postulate: "When an axon of cell A is near enough to excite a cell B and repeatedly or persistently takes part in firing it, some growth process or metabolic change takes place in one or both cells such that A's efficiency, as one of the cells firing B, is increased."

Linear Associator: $a = \text{purelin}(Wp)$

The Hebb Rule: Supervised Form: $w_{ij}^{new} = w_{ij}^{old} + t_{qi} p_{qi}$

$$W = t_1 P_1^T + t_2 P_2^T + \dots + t_Q P_Q^T$$

$$W = [t_1 \ t_2 \ \dots \ t_Q] \begin{bmatrix} P_1^T \\ P_2^T \\ \vdots \\ P_Q^T \end{bmatrix} = TP^T$$

Pseudoinverse Rule: $W = TP^+$

When the number, R , of rows of P is greater than the number of columns, Q , of P and the columns of P are independent, then the pseudoinverse can be computed by $P^+ = (P^T P)^{-1} P^T$

Variations of Hebbian Learning:

Filtered Learning (Ch.14): $W^{new} = (1 - \gamma)W^{old} + \alpha t_q p_q^T$

Delta Rule (Ch.10): $W^{new} = W^{old} + \alpha(t_q - a_q) p_q^T$

Unsupervised Hebb (Ch.13): $W^{new} = W^{old} + \alpha a_q p_q^T$

Taylor: $F(x) = F(x^*) + \nabla F(x^*)^T |_{x=x^*} (x - x^*) + \frac{1}{2} (x - x^*)^T \nabla^2 F(x^*) |_{x=x^*} (x - x^*) + \dots$

Grad $\nabla F(x) = \left[\frac{\partial}{\partial x_1} F(x) \quad \frac{\partial}{\partial x_2} F(x) \quad \dots \quad \frac{\partial}{\partial x_n} F(x) \right]^T$

Hessian: $\nabla^2 F(x) =$

$$\begin{bmatrix} \frac{\partial^2}{\partial x_1^2} F(x) & \frac{\partial^2}{\partial x_1 \partial x_2} F(x) & \dots & \frac{\partial^2}{\partial x_1 \partial x_n} F(x) \\ \frac{\partial^2}{\partial x_2 \partial x_1} F(x) & \frac{\partial^2}{\partial x_2^2} F(x) & \dots & \frac{\partial^2}{\partial x_2 \partial x_n} F(x) \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial^2}{\partial x_n \partial x_1} F(x) & \frac{\partial^2}{\partial x_n \partial x_2} F(x) & \dots & \frac{\partial^2}{\partial x_n^2} F(x) \end{bmatrix}$$

Directional Derivatives:

$$1^{st} \text{ Dir. Der.} = \frac{p^T \nabla F(x)}{\|p\|}, \quad 2^{nd} \text{ Dir. Der.} = \frac{p^T \nabla^2 F(x) p}{\|p\|^2}$$

Minima:

Strong Minimum: if a scalar $\delta > 0$ exists, such that

$F(x) < F(x + \Delta x)$ for all Δx such that $\delta > \|\Delta x\| > 0$.

Global Minimum: if $F(x) < F(x + \Delta x)$ for all $\Delta x \neq 0$

Weak Minimum: if it is not a strong minimum, and a

scalar $\delta > 0$ exists, such that $F(x) \leq F(x + \Delta x)$ for all Δx such that $\delta > \|\Delta x\| > 0$.

Necessary Conditions for Optimality:

1st-Order Condition: $\nabla F(x)|_{x=x^*} = 0$ (Stationary Points)

2nd-Order Condition: $\nabla^2 F(x)|_{x=x^*} \geq 0$ (Positive Semi-definite Hessian Matrix).

Quadratic fn.: $F(x) = \frac{1}{2} x^T A x + d^T x + c$

$$\nabla F(x) = Ax + d, \quad \nabla^2 F(x) = A, \quad \lambda_{min} \leq \frac{p^T A p}{\|p\|^2} \leq \lambda_{max}$$

| | |
|---|---|
| <p>General Minimization Algorithm: $\mathbf{x}_{k+1} = \mathbf{x}_k + \alpha_k \mathbf{p}_k$ or $\Delta \mathbf{x}_k = (\mathbf{x}_{k+1} - \mathbf{x}_k) = \alpha_k \mathbf{p}_k$</p> <p>Steepest Descent Algorithm: $\mathbf{x}_{k+1} = \mathbf{x}_k - \alpha_k \mathbf{g}_k$ where, $\mathbf{g}_k = \nabla F(\mathbf{x}) _{\mathbf{x}=\mathbf{x}_k}$</p> <p>Stable Learning Rate: ($\alpha_k = \alpha$, constant) $\alpha < \frac{2}{\lambda_{max}}$ $\{\lambda_1, \lambda_2, \dots, \lambda_n\}$ Eigenvalues of Hessian matrix A</p> <p>Learning Rate to Minimize Along the Line: $\mathbf{x}_{k+1} = \mathbf{x}_k + \alpha_k \mathbf{p}_k \Rightarrow \alpha_k = -\frac{\mathbf{g}_k^T \mathbf{p}_k}{\mathbf{p}_k^T \mathbf{A} \mathbf{p}_k}$ (For quadratic fn.)</p> <p>After Minimization Along the Line: $\mathbf{x}_{k+1} = \mathbf{x}_k + \alpha_k \mathbf{p}_k \Rightarrow \mathbf{g}_{k+1}^T \mathbf{p}_k = 0$</p> | <p>*Heuristic Variations of Backpropagation:</p> <p>Batching: The parameters are updated only after the entire training set has been presented. The gradients calculated for each training example are averaged together to produce a more accurate estimate of the gradient. (If the training set is complete, i.e., covers all possible input/output pairs, then the gradient estimate will be exact.)</p> <p>Backpropagation with Momentum (MOBP): $\Delta \mathbf{W}^m(k) = \gamma \Delta \mathbf{W}^m(k-1) - (1-\gamma) \alpha \mathbf{s}^m (\mathbf{a}^{m-1})^T$ $\Delta \mathbf{b}^m(k) = \gamma \Delta \mathbf{b}^m(k-1) - (1-\gamma) \alpha \mathbf{s}^m$</p> <p>Variable Learning Rate Backpropagation (VLBP) 1. If the squared error (over the entire training set) increases by more than some set percentage ζ (typically one to five percent) after a weight update, then the weight update is discarded, the learning rate is multiplied by some factor $\rho < 1$, and the momentum coefficient γ (if it is used) is set to zero. 2. If the squared error decreases after a weight update, then the weight update is accepted and the learning rate is multiplied by some factor $\eta > 1$. If γ has been previously set to zero, it is reset to its original value. 3. If the squared error increases by less than ζ, then the weight update is accepted but the learning rate and the momentum coefficient are unchanged.</p> |
| <p>ADALINE: a = purelin(Wp + b)</p> <p>Mean Square Error: (for ADALINE it is a quadratic fn.) $F(\mathbf{x}) = E[e^2] = E[(t - a)^2] = E[(t - \mathbf{x}^T \mathbf{z})^2]$ $F(\mathbf{x}) = c - 2\mathbf{x}^T \mathbf{h} + \mathbf{x}^T \mathbf{R} \mathbf{x}$, $c = E[t^2]$, $\mathbf{h} = E[t\mathbf{z}]$ and $\mathbf{R} = E[\mathbf{z}\mathbf{z}^T] \Rightarrow \Lambda = 2\mathbf{R}$, $\mathbf{d} = -2\mathbf{h}$ Unique minimum, if it exists, is $\mathbf{x}^* = \mathbf{R}^{-1} \mathbf{h}$, where $\mathbf{x} = \begin{bmatrix} \mathbf{1} \mathbf{w} \\ b \end{bmatrix}$ and $\mathbf{z} = \begin{bmatrix} \mathbf{p} \\ 1 \end{bmatrix}$</p> <p>LMS Algorithm: $\mathbf{W}(k+1) = \mathbf{W}(k) + 2\alpha \mathbf{e}(k) \mathbf{p}^T(k)$ $\mathbf{b}(k+1) = \mathbf{b}(k) + 2\alpha \mathbf{e}(k)$</p> <p>Convergence Point: $\mathbf{x}^* = \mathbf{R}^{-1} \mathbf{h}$</p> <p>Stable Learning Rate: $0 < \alpha < 1/\lambda_{max}$ where λ_{max} is the maximum eigenvalue of R</p> <p>Adaptive Filter ADALINE: $a(k) = \text{purelin}(\mathbf{W}\mathbf{p}(k) + b) = \sum_{i=1}^R \mathbf{w}_{i,i} y(k-i+1) + b$</p> | <p>Association: a = hardlim(W⁰p⁰ + Wp + b) An association is a link between the inputs and outputs of a network so that when a stimulus A is presented to the network, it will output a response B.</p> <p>Associative Learning Rules:</p> <p>Unsupervised Hebb Rule: $\mathbf{W}(q) = \mathbf{W}(q-1) + \alpha \mathbf{a}(q) \mathbf{p}^T(q)$</p> <p>Hebb with Decay: $\mathbf{W}(q) = (1-\gamma) \mathbf{W}(q-1) + \alpha \mathbf{a}(q) \mathbf{p}^T(q)$</p> <p>Instar: a = hardlim(Wp + b), a = hardlim(₁w^Tp + b) The instar is activated for ${}_1\mathbf{w}^T \mathbf{p} = \ \mathbf{p}\ \ \mathbf{w}\ \cos \theta \geq -b$ where θ is the angle between \mathbf{p} and ${}_1\mathbf{w}$.</p> <p>Instar Rule: ${}_i\mathbf{w}(q) = {}_i\mathbf{w}(q-1) + \alpha a_i(q) (\mathbf{p}(q) - {}_i\mathbf{w}(q-1))$ ${}_i\mathbf{w}(q) = (1-\alpha) {}_i\mathbf{w}(q-1) + \alpha \mathbf{p}(q)$, if $(a_i(q) = 1)$</p> <p>Kohonen Rule: ${}_i\mathbf{w}(q) = {}_i\mathbf{w}(q-1) + \alpha (\mathbf{p}(q) - {}_i\mathbf{w}(q-1))$ for $i \in X(q)$</p> <p>Outstar Rule: a = satlins(Wp) $\mathbf{w}_j(q) = \mathbf{w}_j(q-1) + \alpha (\mathbf{a}(q) - \mathbf{w}_j(q-1)) p_j(q)$</p> |
| <p>Backpropagation Algorithm:</p> <p>Performance Index: Mean Square error: $F(\mathbf{x}) = E[\mathbf{e}^T \mathbf{e}] = E[(\mathbf{t} - \mathbf{a})^T (\mathbf{t} - \mathbf{a})]$</p> <p>Approximate Performance Index: (single sample) $\hat{F}(\mathbf{x}) = \mathbf{e}^T(k) \mathbf{e}(k) = (\mathbf{t}(k) - \mathbf{a}(k))^T (\mathbf{t}(k) - \mathbf{a}(k))$</p> <p>Sensitivity: $\mathbf{s}^m = \frac{\partial \hat{F}}{\partial \mathbf{n}^m} = \begin{bmatrix} \frac{\partial \hat{F}}{\partial n_1^m} & \frac{\partial \hat{F}}{\partial n_2^m} & \dots & \frac{\partial \hat{F}}{\partial n_{s^m}^m} \end{bmatrix}^T$</p> <p>Forward Propagation: $\mathbf{a}^0 = \mathbf{p}$, $\mathbf{a}^{m+1} = \mathbf{f}^{m+1}(\mathbf{W}^{m+1} \mathbf{a}^m + \mathbf{b}^{m+1})$ for $m = 0, 1, \dots, M-1$ $\mathbf{a} = \mathbf{a}^M$</p> <p>Backward Propagation: $\mathbf{s}^M = -2\hat{\mathbf{F}}^M(\mathbf{n}^M)(\mathbf{t} - \mathbf{a})$, $\mathbf{s}^m = \hat{\mathbf{F}}^m(\mathbf{n}^m)(\mathbf{W}^{m+1})^T \mathbf{s}^{m+1}$ for $m = M-1, \dots, 2, 1$, where $\hat{\mathbf{F}}^m(\mathbf{n}^m) = \text{diag}([\hat{f}^m(n_1^m) \quad \hat{f}^m(n_2^m) \quad \dots \quad \hat{f}^m(n_{s^m}^m)])$ $\hat{f}^m(n_j^m) = \frac{\partial \hat{f}^m(n_j^m)}{\partial n_j^m}$</p> <p>Weight Update (Approximate Steepest Descent): $\mathbf{W}^m(k+1) = \mathbf{W}^m(k) - \alpha \mathbf{s}^m (\mathbf{a}^{m-1})^T$ $\mathbf{b}^m(k+1) = \mathbf{b}^m(k) - \alpha \mathbf{s}^m$</p> | <p>Competitive Layer: a = compet(Wp) = compet(n)</p> <p>Competitive Learning with the Kohonen Rule: ${}_i\mathbf{w}(q) = {}_i\mathbf{w}(q-1) + \alpha (\mathbf{p}(q) - {}_i\mathbf{w}(q-1))$ $= (1-\alpha) {}_i\mathbf{w}(q-1) + \alpha \mathbf{p}(q)$ ${}_i\mathbf{w}(q) = {}_i\mathbf{w}(q-1)$, $i \neq i^*$ where i^* is the winning neuron.</p> <p>Self-Organizing with the Kohonen Rule: ${}_i\mathbf{w}(q) = {}_i\mathbf{w}(q-1) + \alpha (\mathbf{p}(q) - {}_i\mathbf{w}(q-1))$ $= (1-\alpha) {}_i\mathbf{w}(q-1) + \alpha \mathbf{p}(q)$, $i \in N_{i^*}(d)$ $N_{i^*}(d) = \{j, d_{i,j} \leq d\}$</p> <p>LVO Network: ($w_{k,i}^2 = 1$) \Rightarrow subclass i is a part of class k $n_i^1 = -\ {}_i\mathbf{w}^1 - \mathbf{p}\$, $\mathbf{a}^1 = \text{compet}(n^1)$, $\mathbf{a}^2 = \mathbf{W}^2 \mathbf{a}^1$</p> <p>LVQ Network Learning with the Kohonen Rule: ${}_i\mathbf{w}^1(q) = {}_i\mathbf{w}^1(q-1) + \alpha (\mathbf{p}(q) - {}_i\mathbf{w}^1(q-1))$, if $a_k^2 = t_k^* = 1$ ${}_i\mathbf{w}^1(q) = {}_i\mathbf{w}^1(q-1) - \alpha (\mathbf{p}(q) - {}_i\mathbf{w}^1(q-1))$, if $a_k^2 = 1 \neq t_k^* = 0$</p> |
| <p>hardlim: a = $\begin{cases} 0 & n < 0 \\ 1 & n \geq 0 \end{cases}$, hardlims: a = $\begin{cases} -1 & n < 0 \\ +1 & n \geq 0 \end{cases}$, purelin: a = n, Logsig: a = $\frac{1}{1+e^{-n}}$, tanstig: a = $\frac{e^n - e^{-n}}{e^n + e^{-n}}$, postlin: a = $\begin{cases} 0 & n < 0 \\ n & n \geq 0 \end{cases}$</p> <p>compet: a = $\begin{cases} 1 & \text{neuron with max } n \\ 0 & \text{all other neurons} \end{cases}$, satlin: a = $\begin{cases} 0 & n < 0 \\ n & -1 \leq n \leq 1 \\ 1 & n > 1 \end{cases}$, satlins: a = $\begin{cases} -1 & n < 0 \\ -1 \leq n \leq 1 \\ 1 & n > 1 \end{cases}$</p> <p>Delay: a(t) = u(t-1), Integrator: a(t) = $\int_0^t u(\tau) d\tau + a(0)$</p> | <p>**HINT:</p> $\text{diag}([1 \ 2 \ 3]) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$ |

MACHINE LEARNING IN EMOJI


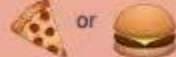
SUPERVISED

UNSUPERVISED

REINFORCEMENT

- SUPERVISED** human builds model based on input / output
- UNSUPERVISED** human input, machine output
human utilizes if satisfactory
- REINFORCEMENT** human input, machine output
human reward/punish, cycle continues

BASIC REGRESSION

- LINEAR** `linear_model.LinearRegression()`
Lots of numerical data 
- LOGISTIC** `linear_model.LogisticRegression()`
Target variable is categorical 





CLASSIFICATION

- NEURAL NET** `neural_network.MLPClassifier()`
Complex relationships. Prone to overfitting
Basically magic. 
- K-NN** `neighbors.KNeighborsClassifier()`
Group membership based on proximity 
- DECISION TREE** `tree.DecisionTreeClassifier()`
If/then/else. Non-contiguous data
Can also be regression 
- RANDOM FOREST** `ensemble.RandomForestClassifier()`
Find best split randomly
Can also be regression 
- SVM** `svm.SVC()` `svm.LinearSVC()`
Maximum margin classifier. Fundamental
Data Science algorithm 
- NAIVE BAYES** `GaussianNB()` `MultinomialNB()` `BernoulliNB()`
Updating knowledge step by step with new info 

CLUSTER ANALYSIS

- K-MEANS** `cluster.KMeans()`
Similar datum into groups
based on centroids 
- ANOMALY DETECTION** `covariance.EllipticalEnvelope()`
Finding outliers
through grouping 

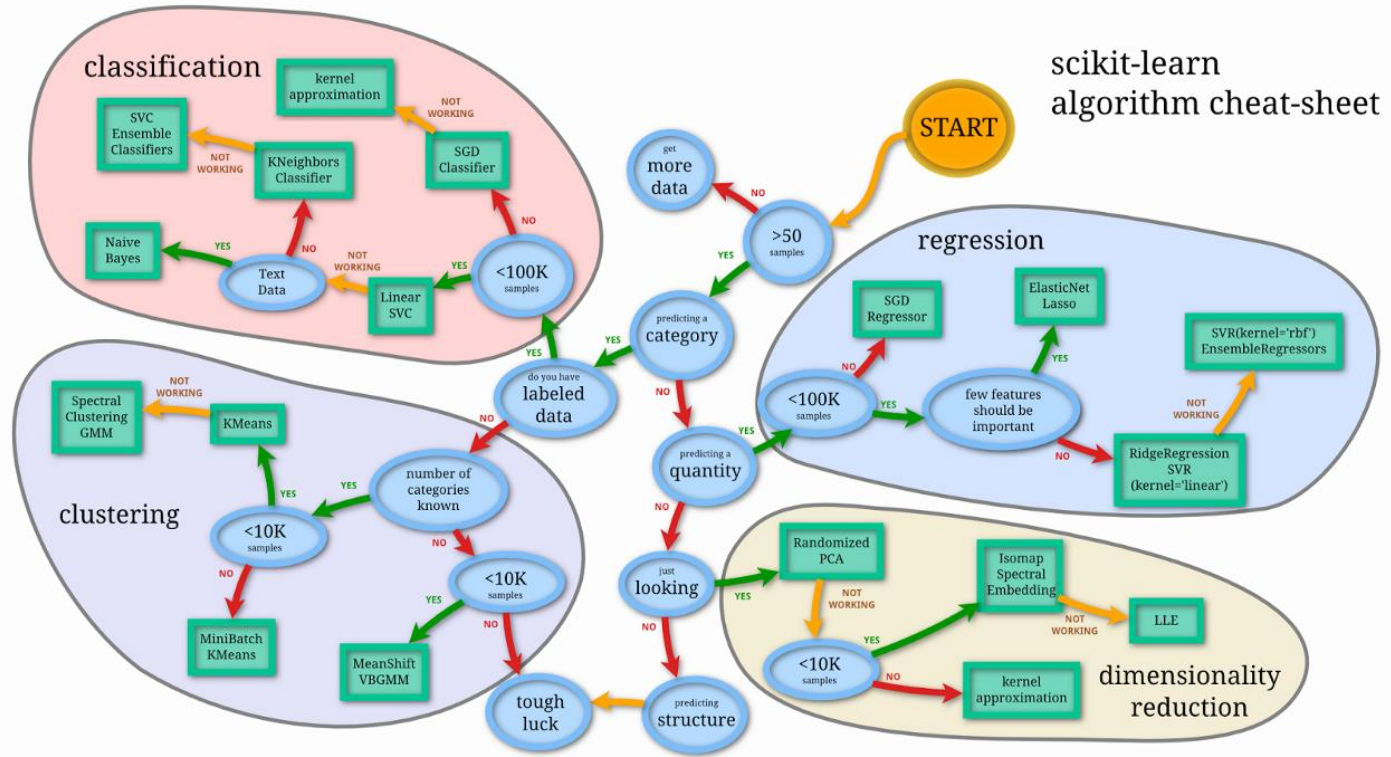
FEATURE REDUCTION

- T-DISTRIBUTION STOCHASTIC NEIB EMBEDDING** `manifold.TSNE()`
Visualize high dimensional data. Convert
similarity to joint probabilities 
- PRINCIPLE COMPONENT ANALYSIS** `decomposition.PCA()`
Distill feature space into components that
describe greatest variance 
- CANONICAL CORRELATION ANALYSIS** `decomposition.CCA()`
Making sense of cross-correlation
matrices 
- LINEAR DISCRIMINANT ANALYSIS** `lda.LDA()`
Linear combination of features that
separates classes 

OTHER IMPORTANT CONCEPTS

- BIAS VARIANCE TRADEOFF** 
- UNDERFITTING / OVERFITTING** 
- INERTIA** 
- ACCURACY FUNCTION** $(TP + TN) / (P + N)$ 
- PRECISION FUNCTION** $TP / (TP + FP)$ 
- SPECIFICITY FUNCTION** $TN / (FP + TN)$ 
- SENSITIVITY FUNCTION** $TP / (TP + FN)$ 

@emilynamillion made this



Python For Data Science Cheat Sheet

Scikit-Learn

Learn Python for data science interactively at www.DataCamp.com



Scikit-learn

Scikit-learn is an open source Python library that implements a range of machine learning, preprocessing, cross-validation and visualization algorithms using a unified interface.



A Basic Example

```
>>> from sklearn import neighbors, datasets, preprocessing
>>> from sklearn.cross_validation import train_test_split
>>> from sklearn.metrics import accuracy_score
>>> iris = datasets.load_iris()
>>> X, y = iris.data[:, :2], iris.target
>>> X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=33)
>>> scaler = preprocessing.StandardScaler().fit(X_train)
>>> X_train = scaler.transform(X_train)
>>> X_test = scaler.transform(X_test)
>>> knn = neighbors.KNeighborsClassifier(n_neighbors=5)
>>> knn.fit(X_train, y_train)
>>> y_pred = knn.predict(X_test)
>>> accuracy_score(y_test, y_pred)
```

Loading The Data

Also see NumPy & Pandas

Your data needs to be numeric and stored as NumPy arrays or SciPy sparse matrices. Other types that are convertible to numeric arrays, such as Pandas DataFrame, are also acceptable.

```
>>> import numpy as np
>>> X = np.random.random((10,5))
>>> y = np.array(['M', 'M', 'F', 'F', 'M', 'F', 'M', 'F', 'F', 'F'])
>>> X[X < 0.7] = 0
```

Training And Test Data

```
>>> from sklearn.cross_validation import train_test_split
>>> X_train, X_test, y_train, y_test = train_test_split(X,
                                                    y,
                                                    random_state=0)
```

Preprocessing The Data

Standardization

```
>>> from sklearn.preprocessing import StandardScaler
>>> scaler = StandardScaler().fit(X_train)
>>> standardized_X = scaler.transform(X_train)
>>> standardized_X_test = scaler.transform(X_test)
```

Normalization

```
>>> from sklearn.preprocessing import Normalizer
>>> scaler = Normalizer().fit(X_train)
>>> normalized_X = scaler.transform(X_train)
>>> normalized_X_test = scaler.transform(X_test)
```

Binarization

```
>>> from sklearn.preprocessing import Binarizer
>>> binarizer = Binarizer(threshold=0.0).fit(X)
>>> binary_X = binarizer.transform(X)
```

Create Your Model

Supervised Learning Estimators

Linear Regression

```
>>> from sklearn.linear_model import LinearRegression
>>> lr = LinearRegression(normalize=True)
```

Support Vector Machines (SVM)

```
>>> from sklearn.svm import SVC
>>> svc = SVC(kernel='linear')
```

Naive Bayes

```
>>> from sklearn.naive_bayes import GaussianNB
>>> gnb = GaussianNB()
```

KNN

```
>>> from sklearn.neighbors import KNeighborsClassifier
>>> knn = neighbors.KNeighborsClassifier(n_neighbors=5)
```

Unsupervised Learning Estimators

Principal Component Analysis (PCA)

```
>>> from sklearn.decomposition import PCA
>>> pca = PCA(n_components=0.95)
```

K Means

```
>>> from sklearn.cluster import KMeans
>>> k_means = KMeans(n_clusters=3, random_state=0)
```

Model Fitting

Supervised learning

```
>>> lr.fit(X, y)
>>> knn.fit(X_train, y_train)
>>> svc.fit(X_train, y_train)
```

Fit the model to the data

Unsupervised Learning

```
>>> k_means.fit(X_train)
>>> pca_model = pca.fit_transform(X_train)
```

Fit the model to the data
Fit to data, then transform it

Prediction

Supervised Estimators

```
>>> y_pred = svc.predict(np.random.random((2,5)))
>>> y_pred = lr.predict(X_test)
>>> y_pred = knn.predict_probs(X_test)
```

Predict labels
Predict labels
Estimate probability of a label

Unsupervised Estimators

```
>>> y_pred = k_means.predict(X_test)
```

Predict labels in clustering algos

Evaluate Your Model's Performance

Classification Metrics

Accuracy Score

```
>>> knn.score(X_test, y_test)
>>> from sklearn.metrics import accuracy_score
>>> accuracy_score(y_test, y_pred)
```

Estimator score method
Metric scoring functions

Classification Report

```
>>> from sklearn.metrics import classification_report
>>> print(classification_report(y_test, y_pred))
```

Precision, recall, f1-score and support

Confusion Matrix

```
>>> from sklearn.metrics import confusion_matrix
>>> print(confusion_matrix(y_test, y_pred))
```

Regression Metrics

Mean Absolute Error

```
>>> from sklearn.metrics import mean_absolute_error
>>> y_true = [3, -0.5, 2]
>>> mean_absolute_error(y_true, y_pred)
```

Mean Squared Error

```
>>> from sklearn.metrics import mean_squared_error
>>> mean_squared_error(y_test, y_pred)
```

R² Score

```
>>> from sklearn.metrics import r2_score
>>> r2_score(y_true, y_pred)
```

Clustering Metrics

Adjusted Rand Index

```
>>> from sklearn.metrics import adjusted_rand_score
>>> adjusted_rand_score(y_true, y_pred)
```

Homogeneity

```
>>> from sklearn.metrics import homogeneity_score
>>> homogeneity_score(y_true, y_pred)
```

V-measure

```
>>> from sklearn.metrics import v_measure_score
>>> metrics.v_measure_score(y_true, y_pred)
```

Cross-Validation

```
>>> from sklearn.cross_validation import cross_val_score
>>> print(cross_val_score(knn, X_train, y_train, cv=4))
>>> print(cross_val_score(lr, X, y, cv=2))
```

Tune Your Model

Grid Search

```
>>> from sklearn.grid_search import GridSearchCV
>>> params = {"n_neighbors": np.arange(1,3),
            "metric": ["euclidean", "cityblock"]}
>>> grid = GridSearchCV(estimator=knn,
                    param_grid=params)
>>> grid.fit(X_train, y_train)
>>> print(grid.best_score_)
>>> print(grid.best_estimator_.n_neighbors)
```

Randomized Parameter Optimization

```
>>> from sklearn.grid_search import RandomizedSearchCV
>>> params = {"n_neighbors": range(1,5),
            "weights": ["uniform", "distance"]}
>>> rsearch = RandomizedSearchCV(estimator=knn,
                             param_distributions=params,
                             cv=4,
                             n_iter=8,
                             random_state=5)
>>> rsearch.fit(X_train, y_train)
>>> print(rsearch.best_score_)
```

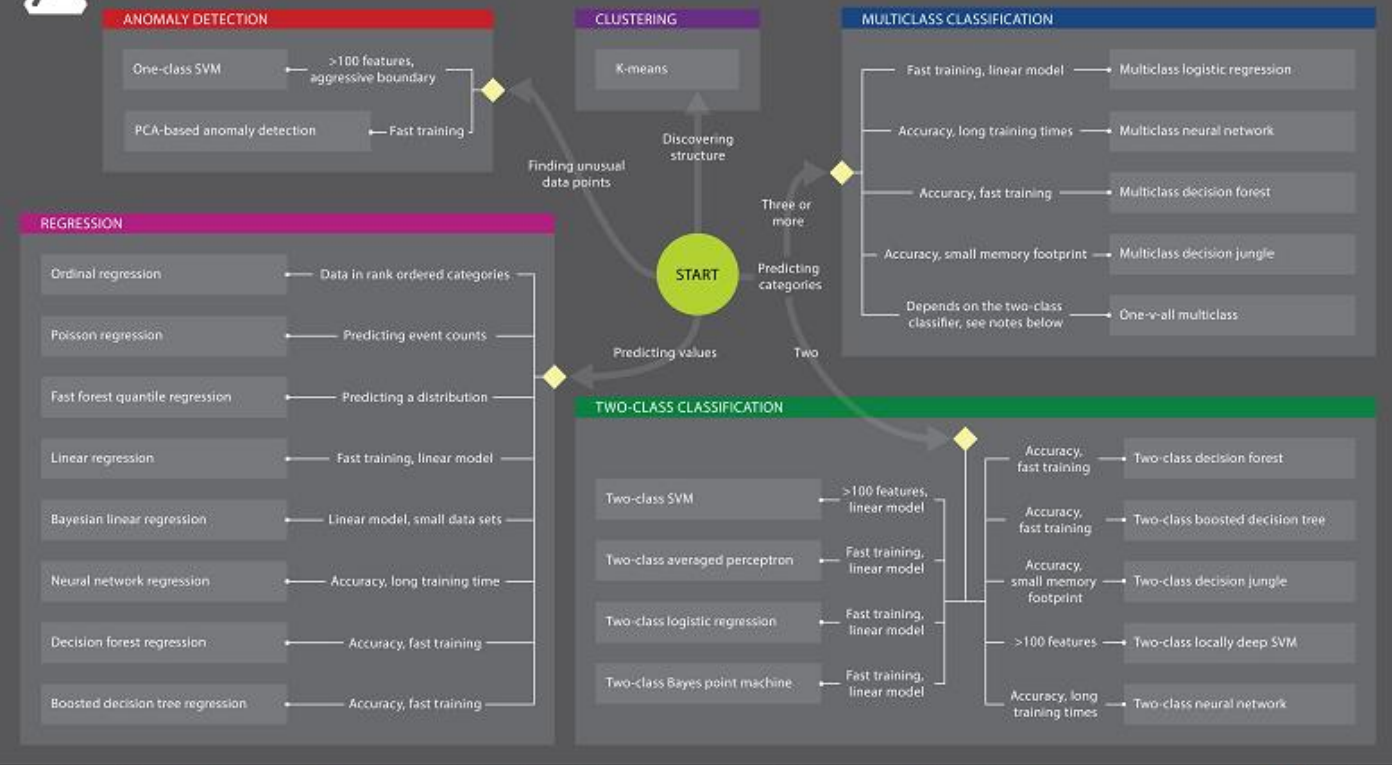
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Learn Python for Data Science Interactively



Microsoft Azure Machine Learning: Algorithm Cheat Sheet

This cheat sheet helps you choose the best Azure Machine Learning Studio algorithm for your predictive analytics solution. Your decision is driven by both the nature of your data and the question you're trying to answer.



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Python For Data Science Cheat Sheet

Python Basics

Learn More Python for Data Science Interactively at www.datacamp.com



Variables and Data Types

Variable Assignment

```
>>> x=5
>>> x
5
```

Calculations With Variables

| | | |
|----------------|-----|---------------------------------|
| >>> x+2 | 7 | Sum of two variables |
| >>> x-2 | 3 | Subtraction of two variables |
| >>> x*2 | 10 | Multiplication of two variables |
| >>> x**2 | 25 | Exponentiation of a variable |
| >>> x%2 | 1 | Remainder of a variable |
| >>> x/float(2) | 2.5 | Division of a variable |

Types and Type Conversion

| | | |
|---------|---------------------|-----------------------|
| str() | '5', '3.45', 'True' | Variables to strings |
| int() | 5, 3, 1 | Variables to integers |
| float() | 5.0, 1.0 | Variables to floats |
| bool() | True, True, True | Variables to booleans |

Asking For Help

```
>>> help(str)
```

Strings

```
>>> my_string = 'thisStringIsAwesome'
>>> my_string
'thisStringIsAwesome'
```

String Operations

```
>>> my_string * 2
'thisStringIsAwesomethisStringIsAwesome'
>>> my_string + 'Innit'
'thisStringIsAwesomeInnit'
>>> 'm' in my_string
True
```

Lists

Also see NumPy Arrays

```
>>> a = 'is'
>>> b = 'nice'
>>> my_list = ['my', 'list', a, b]
>>> my_list2 = [[4,5,6,7], [3,4,5,6]]
```

Selecting List Elements

Index starts at 0

| | |
|------------------------------|--|
| Subset | Select item at index 1 Select 3rd last item |
| >>> my_list[1] | |
| >>> my_list[-3] | |
| Slice | Select items at index 1 and 2 Select items after index 0 Select items before index 3 Copy my_list |
| >>> my_list[1:3] | |
| >>> my_list[1:] | |
| >>> my_list[:3] | |
| >>> my_list[:] | |
| Subset Lists of Lists | my_list[listOfItemOfList] |
| >>> my_list2[1][0] | |
| >>> my_list2[1][:2] | |

List Operations

```
>>> my_list + my_list
['my', 'list', 'is', 'nice', 'my', 'list', 'is', 'nice']
>>> my_list * 2
['my', 'list', 'is', 'nice', 'my', 'list', 'is', 'nice']
>>> my_list2 > 4
True
```

List Methods

| | |
|----------------------------|--------------------------|
| >>> my_list.index(a) | Get the index of an item |
| >>> my_list.count(a) | Count an item |
| >>> my_list.append('!') | Append an item at a time |
| >>> my_list.remove('!') | Remove an item |
| >>> del(my_list[0:1]) | Remove an item |
| >>> my_list.reverse() | Reverse the list |
| >>> my_list.extend('!') | Append an item |
| >>> my_list.pop(-1) | Remove an item |
| >>> my_list.insert(0, '!') | Insert an item |
| >>> my_list.sort() | Sort the list |

String Operations

Index starts at 0

```
>>> my_string[3]
'i'
>>> my_string[4:9]
'ngIsAwes'
```

String Methods

| | |
|---------------------------------|----------------------------|
| >>> my_string.upper() | String to uppercase |
| >>> my_string.lower() | String to lowercase |
| >>> my_string.count('w') | Count String elements |
| >>> my_string.replace('e', 'i') | Replace String elements |
| >>> my_string.strip() | Strip whitespace from ends |

Libraries

Import libraries

```
>>> import numpy
>>> import numpy as np
Selective import
>>> from math import pi
```



Install Python



NumPy Arrays

Also see Lists

```
>>> my_list = [1, 2, 3, 4]
>>> my_array = np.array(my_list)
>>> my_2darray = np.array([[1,2,3], [4,5,6]])
```

Selecting NumPy Array Elements

Index starts at 0

| | |
|-------------------------------|-------------------------------|
| Subset | Select item at index 1 |
| >>> my_array[1] | 2 |
| Slice | Select items at index 0 and 1 |
| >>> my_array[0:2] | array([1, 2]) |
| Subset 2D NumPy arrays | my_2darray[rows, columns] |
| >>> my_2darray[:,0] | array([1, 4]) |

NumPy Array Operations

```
>>> my_array > 3
array([False, False, False,  True], dtype=bool)
>>> my_array * 2
array([2, 4, 6, 8])
>>> my_array + np.array([5, 6, 7, 8])
array([16, 8, 10, 12])
```

NumPy Array Functions

| | |
|-------------------------------|---------------------------------|
| >>> my_array.shape | Get the dimensions of the array |
| >>> np.append(other_array) | Append items to an array |
| >>> np.insert(my_array, 1, 5) | Insert items in an array |
| >>> np.delete(my_array, [1]) | Delete items in an array |
| >>> np.mean(my_array) | Mean of the array |
| >>> np.median(my_array) | Median of the array |
| >>> my_array.corrcoef() | Correlation coefficient |
| >>> np.std(my_array) | Standard deviation |

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Bokeh

Learn Bokeh Interactively at www.DataCamp.com,
taught by Bryan Van de Ven, core contributor



Plotting With Bokeh

The Python interactive visualization library Bokeh enables high-performance visual presentation of large datasets in modern web browsers.



Bokeh's mid-level general purpose `bokeh.plotting` interface is centered around two main components: data and glyphs.



The basic steps to creating plots with the `bokeh.plotting` interface are:

1. Prepare some data: Python lists, NumPy arrays, Pandas DataFrames and other sequences of values
2. Create a new plot
3. Add renderers for your data, with visual customizations
4. Specify where to generate the output
5. Show or save the results

```
>>> from bokeh.plotting import figure
>>> from bokeh.io import output_file, show
>>> x = [1, 2, 3, 4, 5]
>>> y = [6, 7, 2, 4, 5]
>>> p = figure(title="simple line example",
>>>             x_axis_label='x',
>>>             y_axis_label='y')
>>> p.line(x, y, legend="Temp.", line_width=2)
>>> output_file("lines.html")
>>> show(p)
```

1 Data

Also see Lists, NumPy & Pandas

Under the hood, your data is converted to Column Data Sources. You can also do this manually:

```
>>> import numpy as np
>>> import pandas as pd
>>> df = pd.DataFrame(np.array([[33.9, 4, 65, 'US'],
>>>                             [32.4, 4, 66, 'Asia'],
>>>                             [21.4, 4, 109, 'Europe']]},
>>>                  columns=['mpg', 'cyl', 'hp', 'origin'],
>>>                  index=['Toyota', 'Fiat', 'Volvo'])
>>> from bokeh.models import ColumnDataSource
>>> cds_df = ColumnDataSource(df)
```

2 Plotting

```
>>> from bokeh.plotting import figure
>>> p1 = figure(plot_width=300, tools='pan,box_zoom')
>>> p2 = figure(plot_width=300, plot_height=300,
>>>             x_range=(0, 8), y_range=(0, 8))
>>> p3 = figure()
```

3 Renderers & Visual Customizations

Glyphs

```
Scatter Markers
>>> p1.circle(np.array([1,2,3]), np.array([3,2,1]),
>>>           fill_color="white")
>>> p2.square(np.array([1.5,3.5,5.5]), [1,4,3],
>>>           color="blue", size=1)

Line Glyphs
>>> p1.line([1,2,3,4], [3,4,5,6], line_width=2)
>>> p2.multi_line(pd.DataFrame([[1,2,3],[5,6,7]]),
>>>               pd.DataFrame([[3,4,5],[3,2,1]]),
>>>               color="blue")
```

Rows & Columns Layout

```
Rows
>>> from bokeh.layouts import row
>>> layout = row(p1,p2,p3)

Columns
>>> from bokeh.layouts import columns
>>> layout = column(p1,p2,p3)

Nesting Rows & Columns
>>> layout = row(column(p1,p2), p3)
```

Grid Layout

```
>>> from bokeh.layouts import gridplot
>>> row1 = [p1,p2]
>>> row2 = [p3]
>>> layout = gridplot([[p1,p2],[p3]])
```

Tabbed Layout

```
>>> from bokeh.models.widgets import Panel, Tabs
>>> tab1 = Panel(child=p1, title="tab1")
>>> tab2 = Panel(child=p2, title="tab2")
>>> layout = Tabs(tabs=[tab1, tab2])
```

Legends

Legend Location

```
Inside Plot Area
>>> p.legend.location = 'bottom_left'

Outside Plot Area
>>> r1 = p2.asterisk(np.array([1,2,3]), np.array([3,2,1])
>>> r2 = p2.line([1,2,3,4], [3,4,5,6])
>>> legend = Legend(items=[("One", [p1, r1]), ("Two", [r2])], location=(0, -30))
>>> p.add_layout(legend, 'right')
```

Customized Glyphs

Also see Data

```
Selection and Non-Selection Glyphs
>>> p.circle('mpg', 'cyl', source=cds_df,
>>>          selection_color='red',
>>>          nonselection_alpha=0.1)

Hover Glyphs
>>> hover = HoverTool(tooltips=None, mode='vline')
>>> p.add_tools(hover)

Colormapping
>>> color_mapper = CategoricalColorMapper(
>>>     factors=['Europe', 'Asia', 'US'],
>>>     palette=['red', 'green', 'blue'])
>>> p.circle('mpg', 'cyl', source=cds_df,
>>>          color=dict(field='origin',
>>>                    transform=color_mapper),
>>>          legend='Origin')
```

Linked Plots

Linked Axes

```
>>> p2.x_range = p1.x_range
>>> p2.y_range = p1.y_range
```

Linked Brushing

```
>>> p4 = figure(plot_width = 100, tools='box_select,lasso_select')
>>> p4.circle('mpg', 'cyl', source=cds_df)
>>> p5 = figure(plot_width = 200, tools='box_select,lasso_select')
>>> p5.circle('mpg', 'hp', source=cds_df)
>>> layout = row(p4,p5)
```

4 Output

Output to HTML File

```
>>> from bokeh.io import output_file, show
>>> output_file('my_bar_chart.html', mode='cdn')
```

Notebook Output

```
>>> from bokeh.io import output_notebook, show
>>> output_notebook()
```

Embedding

Standalone HTML

```
>>> from bokeh.embed import file_html
>>> html = file_html(p, CDN, "my_plot")
```

Components

```
>>> from bokeh.embed import components
>>> script, div = components(p)
```

5 Show or Save Your Plots

```
>>> show(p1)
>>> show(layout)

>>> save(p1)
>>> save(layout)
```

Statistical Charts With Bokeh

Also see Data

Bokeh's high-level `bokeh.charts` interface is ideal for quickly creating statistical charts

Bar Chart

```
>>> from bokeh.charts import Bar
>>> p = Bar(df, stacked=True, palette=['red','blue'])
```

Box Plot

```
>>> from bokeh.charts import BoxPlot
>>> p = BoxPlot(df, values='vals', label='cyl',
>>>             legend='bottom_right')
```

Histogram

```
>>> from bokeh.charts import Histogram
>>> p = Histogram(df, title='Histogram')
```

Scatter Plot

```
>>> from bokeh.charts import Scatter
>>> p = Scatter(df, x='mpg', y='hp', marker='square',
>>>             xlabel='Miles Per Gallon',
>>>             ylabel='Horsepower')
```


About

TensorFlow

TensorFlow™ is an open source software library for numerical computation using data flow graphs. TensorFlow was originally developed for the purposes of conducting machine learning and deep neural networks research, but the system is general enough to be applicable in a wide variety of other domains as well.

Skflow

Scikit Flow provides a set of high level model classes that you can use to easily integrate with your existing Scikit-learn pipeline code. Scikit Flow is a simplified interface for TensorFlow, to get people started on predictive analytics and data mining. Scikit Flow has been merged into TensorFlow since version 0.8 and now called TensorFlow Learn.

Keras

Keras is a minimalist, highly modular neural networks library, written in Python and capable of running on top of either TensorFlow or Theano

Installation

How to install new package in Python:

```
pip install <package-name>
```

Example: `pip install requests`

How to install tensorflow?

```
device = cpu/gpu
```

```
python_version = cp27/cp34
```

```
sudo pip install
```

```
https://storage.googleapis.com/tensorflow/linux/$device/tensorflow-0.8.0-$python_version-none-linux_x86_64.whl
```

How to install Skflow

```
pip install sklearn
```

How to install Keras

```
pip install keras
```

update ~/.keras/keras.json - replace "theano" by "tensorflow"

Helpers

Python helper

Important functions

```
type(object)
```

Get object type

```
help(object)
```

Get help for object (list of available methods, attributes, signatures and so on)

```
dir(object)
```

Get list of object attributes (fields, functions)

```
str(object)
```

Transform an object to string

```
object?
```

Shows documentations about the object

```
globals()
```

Return the dictionary containing the current scope's global variables.

```
locals()
```

Update and return a dictionary containing the current scope's local variables.

```
id(object)
```

Return the identity of an object. This is guaranteed to be unique among simultaneously existing objects.

```
import __builtin__
```

```
dir(__builtin__)
```

Other built-in functions

TensorFlow

Main classes

```
tf.Graph()
```

```
tf.Operation()
```

```
tf.Tensor()
```

```
tf.Session()
```

Some useful functions

```
tf.get_default_session()
```

```
tf.get_default_graph()
```

```
tf.reset_default_graph()
```

```
ops.reset_default_graph()
```

```
tf.device("/cpu:0")
```

```
tf.name_scope(value)
```

```
tf.convert_to_tensor(value)
```

TensorFlow Optimizers

```
GradientDescentOptimizer
```

```
AdadeltaOptimizer
```

```
AdagradOptimizer
```

```
MomentumOptimizer
```

```
AdamOptimizer
```

```
FtrlOptimizer
```

```
RMSPropOptimizer
```

Reduction

```
reduce_sum
```

```
reduce_prod
```

```
reduce_min
```

```
reduce_max
```

```
reduce_mean
```

```
reduce_all
```

```
reduce_any
```

```
accumulate_n
```

Activation functions

```
tf.nn?
```

```
relu
```

```
relu6
```

```
elu
```

```
softplus
```

```
softsign
```

```
dropout
```

```
bias_add
```

```
sigmoid
```

```
tanh
```

```
sigmoid_cross_entropy_with_logits
```

```
softmax
```

```
log_softmax
```

```
softmax_cross_entropy_with_logits
```

```
sparse_softmax_cross_entropy_with_logits
```

```
weighted_cross_entropy_with_logits
```

etc.

Skflow

Main classes

```
TensorFlowClassifier
```

```
TensorFlowRegressor
```

```
TensorFlowDNNClassifier
```

```
TensorFlowDNNRegressor
```

```
TensorFlowLinearClassifier
```

```
TensorFlowLinearRegressor
```

```
TensorFlowRNNClassifier
```

```
TensorFlowRNNRegressor
```

TensorFlowEstimator

Each classifier and regressor have following fields

n_classes=0 (Regressor), n_classes are expected to be input (Classifiers)

```
batch_size=32,
```

```
steps=200, // except
```

```
TensorFlowRNNClassifier - there is 50
```

```
optimizer='Adagrad',
```

```
learning_rate=0.1,
```

Python For Data Science Cheat Sheet

Keras

Learn Python for data science interactively at www.DataCamp.com



Keras

Keras is a powerful and easy-to-use deep learning library for Theano and TensorFlow that provides a high-level neural networks API to develop and evaluate deep learning models.

A Basic Example

```
>>> import numpy as np
>>> from keras.models import Sequential
>>> from keras.layers import Dense
>>> data = np.random.random((1000,100))
>>> labels = np.random.randint(2,size=(1000,1))
>>> model = Sequential()
>>> model.add(Dense(32,
>>>                 activation='relu',
>>>                 input_dim=100))
>>> model.add(Dense(1, activation='sigmoid'))
>>> model.compile(optimizer='rmsprop',
>>>               loss='binary_crossentropy',
>>>               metrics=['accuracy'])
>>> model.fit(data, labels, epochs=10, batch_size=32)
>>> predictions = model.predict(data)
```

Data

Also see NumPy, Pandas & Scikit-Learn

Your data needs to be stored as NumPy arrays or as a list of NumPy arrays. Ideally, you split the data in training and test sets, for which you can also resort to the `train_test_split` module of `sklearn.cross_validation`.

Keras Data Sets

```
>>> from keras.datasets import boston_housing,
>>>                               mnist,
>>>                               cifar10,
>>>                               imdb
>>> (x_train,y_train),(x_test,y_test) = mnist.load_data()
>>> (x_train2,y_train2),(x_test2,y_test2) = boston_housing.load_data()
>>> (x_train3,y_train3),(x_test3,y_test3) = cifar10.load_data()
>>> (x_train4,y_train4),(x_test4,y_test4) = imdb.load_data(num_words=20000)
>>> num_classes = 10
```

Other

```
>>> from urllib.request import urlopen
>>> data = np.loadtxt(urlopen('http://archive.ics.uci.edu/
>>> ml/machine-learning-databases/pima-indians-diabetes/
>>> pima-indians-diabetes.data'),delimiter=',')
>>> X = data[:,0:8]
>>> y = data[:,8]
```

Preprocessing

Sequence Padding

```
>>> from keras.preprocessing import sequence
>>> x_train4 = sequence.pad_sequences(x_train4,maxlen=80)
>>> x_test4 = sequence.pad_sequences(x_test4,maxlen=80)
```

One-Hot Encoding

```
>>> from keras.utils import to_categorical
>>> Y_train = to_categorical(y_train, num_classes)
>>> Y_test = to_categorical(y_test, num_classes)
>>> Y_train3 = to_categorical(y_train3, num_classes)
>>> Y_test3 = to_categorical(y_test3, num_classes)
```

Model Architecture

Sequential Model

```
>>> from keras.models import Sequential
>>> model = Sequential()
>>> model2 = Sequential()
>>> model3 = Sequential()
```

Multilayer Perceptron (MLP)

Binary Classification

```
>>> from keras.layers import Dense
>>> model.add(Dense(12,
>>>                 input_dim=8,
>>>                 kernel_initializer='uniform',
>>>                 activation='relu'))
>>> model.add(Dense(8, kernel_initializer='uniform', activation='relu'))
>>> model.add(Dense(1, kernel_initializer='uniform', activation='sigmoid'))
```

Multi-Class Classification

```
>>> from keras.layers import Dropout
>>> model.add(Dense(512, activation='relu', input_shape=(784,)))
>>> model.add(Dropout(0.2))
>>> model.add(Dense(512, activation='relu'))
>>> model.add(Dropout(0.2))
>>> model.add(Dense(10, activation='softmax'))
```

Regression

```
>>> model.add(Dense(64, activation='relu', input_dim=train_data.shape[1]))
>>> model.add(Dense(1))
```

Convolutional Neural Network (CNN)

```
>>> from keras.layers import Activation, Conv2D, MaxPooling2D, Flatten
>>> model2.add(Conv2D(32, (3,3), padding='same', input_shape=x_train.shape[1:]))
>>> model2.add(Activation('relu'))
>>> model2.add(Conv2D(32, (3,3)))
>>> model2.add(Activation('relu'))
>>> model2.add(MaxPooling2D(pool_size=(2,2)))
>>> model2.add(Dropout(0.25))
>>> model2.add(Conv2D(64, (3,3), padding='same'))
>>> model2.add(Activation('relu'))
>>> model2.add(Conv2D(64, (3,3)))
>>> model2.add(Activation('relu'))
>>> model2.add(MaxPooling2D(pool_size=(2,2)))
>>> model2.add(Dropout(0.25))
>>> model2.add(Flatten())
>>> model2.add(Dense(512))
>>> model2.add(Activation('relu'))
>>> model2.add(Dropout(0.5))
>>> model2.add(Dense(num_classes))
>>> model2.add(Activation('softmax'))
```

Recurrent Neural Network (RNN)

```
>>> from keras.layers import Embedding, LSTM
>>> model3.add(Embedding(20000,128))
>>> model3.add(LSTM(128, dropout=0.2, recurrent_dropout=0.2))
>>> model3.add(Dense(1, activation='sigmoid'))
```

Inspect Model

```
>>> model.output_shape
>>> model.summary()
>>> model.get_config()
>>> model.get_weights()
```

Compile Model

MLP: Binary Classification

```
>>> model.compile(optimizer='adam',
>>>               loss='binary_crossentropy',
>>>               metrics=['accuracy'])
```

MLP: Multi-Class Classification

```
>>> model.compile(optimizer='rmsprop',
>>>               loss='categorical_crossentropy',
>>>               metrics=['accuracy'])
```

MLP: Regression

```
>>> model.compile(optimizer='rmsprop',
>>>               loss='mse',
>>>               metrics=['mae'])
```

Recurrent Neural Network

```
>>> model3.compile(loss='binary_crossentropy',
>>>                optimizer='adam',
>>>                metrics=['accuracy'])
```

Model Training

```
>>> model3.fit(x_train4,
>>>            y_train4,
>>>            batch_size=32,
>>>            epochs=15,
>>>            verbose=1,
>>>            validation_data=(x_test4,y_test4))
```

Evaluate Your Model's Performance

```
>>> score = model3.evaluate(x_test,
>>>                          y_test,
>>>                          batch_size=32)
```

Prediction

```
>>> model3.predict(x_test4, batch_size=32)
>>> model3.predict_classes(x_test4, batch_size=32)
```

Save/Reload Models

```
>>> from keras.models import load_model
>>> model3.save('model_h5.h5')
>>> my_model = load_model('my_model.h5')
```

Model Fine-tuning

Optimization Parameters

```
>>> from keras.optimizers import RMSprop
>>> opt = RMSprop(lr=0.0001, decay=1e-6)
>>> model2.compile(loss='categorical_crossentropy',
>>>                optimizer=opt,
>>>                metrics=['accuracy'])
```

Early Stopping

```
>>> from keras.callbacks import EarlyStopping
>>> early_stopping_monitor = EarlyStopping(patience=2)
>>> model3.fit(x_train4,
>>>            y_train4,
>>>            batch_size=32,
>>>            epochs=15,
>>>            validation_data=(x_test4,y_test4),
>>>            callbacks=[early_stopping_monitor])
```

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Python For Data Science Cheat Sheet

Pandas Basics

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Pandas

The Pandas library is built on NumPy and provides easy-to-use data structures and data analysis tools for the Python programming language.



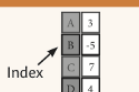
Use the following import convention:

```
>>> import pandas as pd
```

Pandas Data Structures

Series

A one-dimensional labeled array capable of holding any data type



```
>>> s = pd.Series([3, -5, 7, 4], index=['a', 'b', 'c', 'd'])
```

DataFrame

Columns

| | Country | Capital | Population |
|---|---------|-----------|------------|
| a | Belgium | Brussels | 11190846 |
| b | India | New Delhi | 1303171035 |
| c | Brazil | Brasilia | 207847528 |

A two-dimensional labeled data structure with columns of potentially different types

```
>>> data = {'Country': ['Belgium', 'India', 'Brazil'],
>>>          'Capital': ['Brussels', 'New Delhi', 'Brasilia'],
>>>          'Population': [11190846, 1303171035, 207847528]}
>>> df = pd.DataFrame(data,
>>>                   columns=['Country', 'Capital', 'Population'])
```

I/O

Read and Write to CSV

```
>>> pd.read_csv('file.csv', header=None, nrows=5)
>>> pd.to_csv('myDataFrame.csv')
```

Read and Write to Excel

```
>>> pd.read_excel('file.xlsx')
>>> pd.to_excel('dir/myDataFrame.xlsx', sheet_name='Sheet1')
Read multiple sheets from the same file
>>> xlsx = pd.ExcelFile('file.xls')
>>> df = pd.read_excel(xlsx, 'Sheet1')
```

Asking For Help

```
>>> help(pd.Series.loc)
```

Selection

Also see NumPy Arrays

Getting

```
>>> s['b']
-5
Get one element
>>> df[1]
Country Capital Population
1 India New Delhi 1303171035
2 Brazil Brasilia 207847528
Get subset of a DataFrame
```

Selecting, Boolean Indexing & Setting

```
By Position
>>> df.iloc[0], (0)
'Belgium'
Select single value by row & column
>>> df.iat[0], (0)
'Belgium'
By Label
>>> df.loc[0], ['Country']
'Belgium'
Select single value by row & column labels
>>> df.at[0], ['Country']
'Belgium'
By Label/Position
>>> df.ix[2]
Country Brazil
Capital Brasilia
Population 207847528
Select single row of subset of rows
>>> df.ix[:, 'Capital']
0 Brussels
1 New Delhi
2 Brasilia
Select a single column of subset of columns
>>> df.ix[1, 'Capital']
'New Delhi'
Select rows and columns
Boolean Indexing
>>> s[~(s > 1)]
>>> s[(s < -1) | (s > 2)]
>>> df[df['Population'] > 1200000000]
Use filter to adjust DataFrame
Setting
>>> s['a'] = 6
Set index a of Series s to 6
```

Dropping

```
>>> s.drop(['a', 'c'])
Drop values from rows (axis=0)
>>> df.drop('Country', axis=1)
Drop values from columns (axis=1)
```

Sort & Rank

```
>>> df.sort_index(by='Country')
Sort by row or column index
>>> s.order()
Sort a series by its values
>>> df.rank()
Assign ranks to entries
```

Retrieving Series/DataFrame Information

Basic Information

```
>>> df.shape
(rows, columns)
>>> df.index
Describe index
>>> df.columns
Describe DataFrame columns
>>> df.info()
Info on DataFrame
>>> df.count()
Number of non-NA values
```

Summary

```
>>> df.sum()
Sum of values
>>> df.cumsum()
Cumulative sum of values
>>> df.min()/df.max()
Minimum/Maximum values
>>> df.idxmin()/df.idxmax()
Minimum/Maximum index value
>>> df.describe()
Summary statistics
>>> df.mean()
Mean of values
>>> df.median()
Median of values
```

Applying Functions

```
>>> f = lambda x: x*2
>>> df.apply(f)
Apply function
>>> df.applymap(f)
Apply function element-wise
```

Data Alignment

Internal Data Alignment

NA values are introduced in the indices that don't overlap:

```
>>> s3 = pd.Series([7, -2, 3], index=['a', 'c', 'd'])
>>> s + s3
a 10.0
b NaN
c 5.0
d 7.0
```

Arithmetic Operations with Fill Methods

You can also do the internal data alignment yourself with the help of the fill methods:

```
>>> s.add(s3, fill_value=0)
a 10.0
b -5.0
c 5.0
d 7.0
>>> s.sub(s3, fill_value=2)
>>> s.div(s3, fill_value=4)
>>> s.mul(s3, fill_value=3)
```

DataCamp

Learn Python for Data Science Interactively



Python For Data Science Cheat Sheet

NumPy Basics

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NumPy

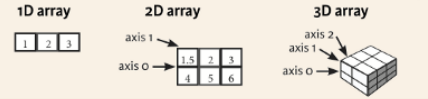
The NumPy library is the core library for scientific computing in Python. It provides a high-performance multidimensional array object, and tools for working with these arrays.



Use the following import convention:

```
>>> import numpy as np
```

NumPy Arrays



Creating Arrays

```
>>> a = np.array([1,2,3])
>>> b = np.array([[1.5,2,3], (4,5,6)], dtype = float)
>>> c = np.array([[1.5,2,3], (4,5,6)], [(3,2,1), (4,5,6)]], dtype = float)
```

Initial Placeholders

```
>>> np.zeros((3,4))
>>> np.ones((2,3,4),dtype=np.int16)
>>> d = np.arange(10,25,5)
>>> np.linspace(0,2,9)
>>> e = np.full((2,2),7)
>>> f = np.eye(2)
>>> np.random.random((2,2))
>>> np.empty((3,2))
```

I/O

Saving & Loading On Disk

```
>>> np.save('my_array', a)
>>> np.savez('array.npz', a, b)
>>> np.load('my_array.npy')
```

Saving & Loading Text Files

```
>>> np.loadtxt('myfile.txt')
>>> np.genfromtxt('my_file.csv', delimiter=',')
>>> np.savetxt('myarray.txt', a, delimiter=" ")
```

Data Types

```
>>> np.int64
>>> np.float32
>>> np.complex
>>> np.bool
>>> np.object
>>> np.string_
>>> np.unicode_
```

Signed 64-bit integer types
Standard double-precision floating point
Complex numbers represented by 128 floats
Boolean type storing TRUE and FALSE values
Python object type
Fixed-length string type
Fixed-length unicode type

Inspecting Your Array

```
>>> a.shape
>>> len(a)
>>> b.ndim
>>> e.size
>>> b.dtype
>>> b.dtype.name
>>> b.astype(int)
```

Array dimensions
Length of array
Number of array dimensions
Number of array elements
Data type of array elements
Name of data type
Convert an array to a different type

Asking For Help

```
>>> np.info(np.ndarray.dtype)
```

Array Mathematics

```
>>> g = a - b
array([[ -0.5,  0. ,  0. ],
       [ -3. , -3. , -3. ]])
>>> np.subtract(a,b)
>>> b + a
array([[ 2.5,  4. ,  6. ],
       [ 5. ,  7. ,  9. ]])
>>> np.add(b,a)
>>> a / b
array([[ 0.6666667,  1. ,  1. ],
       [ 0.25 ,  0.4 ,  0.5 ]])
>>> np.divide(a,b)
>>> a * b
array([[ 1.5,  4. ,  9. ],
       [ 4. , 10. , 18. ]])
>>> np.multiply(a,b)
>>> np.exp(b)
>>> np.sqrt(b)
>>> np.sin(a)
>>> np.cos(a)
>>> np.log(a)
>>> e.dot(f)
array([[ 7. ,  7. ]],
      [[ 7. ,  7. ]])
```

Subtraction
Subtraction
Addition
Addition
Division
Division
Division
Multiplication
Multiplication
Exponentiation
Square root
Print sines of an array
Element-wise cosine
Element-wise natural logarithm
Dot product

Comparison

```
>>> a == b
array([[False,  True,  True],
       [False, False, False]], dtype=bool)
>>> a < 2
array([[True,  False, False],
       [True,  False, False]], dtype=bool)
>>> np.array_equal(a, b)
```

Element-wise comparison
Element-wise comparison
Array-wise comparison

Aggregate Functions

```
>>> a.sum()
>>> a.min()
>>> b.max(axis=0)
>>> b.cumsum(axis=1)
>>> a.mean()
>>> b.median()
>>> a.corrcoef()
>>> np.std(b)
```

Array-wise sum
Array-wise minimum value
Maximum value of an array row
Cumulative sum of the elements
Mean
Median
Correlation coefficient
Standard deviation

Copying Arrays

```
>>> h = a.view()
>>> np.copy(a)
>>> h = a.copy()
```

Create a view of the array with the same data
Create a copy of the array
Create a deep copy of the array

Sorting Arrays

```
>>> a.sort()
>>> c.sort(axis=0)
```

Sort an array
Sort the elements of an array's axis

Subsetting, Slicing, Indexing

Also see Lists

```
>>> a[2]
3
>>> b[1,2]
6.0
>>> b[0:2]
array([1, 2])
>>> b[0:2,1]
array([ 2.,  5.])
>>> b[1:]
array([[1.5, 2., 3.]],
      [[4., 5., 6.]])
>>> a[1, : -1]
array([[3., 2., 1.]])
>>> a[1, ::-1]
array([[3., 2., 1.]])
>>> a[a<2]
array([1])
>>> b[[1, 0, 1, 0], [0, 1, 2, 0]]
array([[4., 2., 6., 1.5]])
>>> b[[1, 0, 1, 0]][[1, 0, 1, 2, 0]]
array([[4., 5., 6., 4.],
       [2.5, 2., 3., 1.5]])
```

Select the element at the 2nd index
Select the element at row 0 column 2 (equivalent to b[0][2])
Select items at index 0 and 1
Select items at rows 0 and 1 in column 1
Select all items at row 0 (equivalent to b[0][:, :])
Same as [1, :, :]
Reversed array a
Select elements from a less than 2
Select elements (1,0,0,1), (1,2) and (0,0)
Select a subset of the matrix's rows and columns

Array Manipulation

```
>>> i = np.transpose(b)
>>> i.T
>>> g.ravel()
>>> g.reshape(3,-2)
>>> h.resize((2,6))
>>> np.append(i, g)
>>> np.insert(a, 1, 5)
>>> np.delete(a, [1])
>>> np.concatenate((a,d),axis=0)
array([ 1,  2,  3, 10, 15, 20])
>>> np.vstack((a,b))
array([[ 1.,  2.,  3. ],
       [ 1.5,  2.,  3. ],
       [ 4.,  5.,  6. ]])
>>> np.r_*(e,f)
array([[ 7.,  7.,  0.,  1. ]])
>>> np.column_stack((a,d))
array([[ 1, 10],
       [ 2, 20],
       [ 3, 20]])
>>> np.c_[a,d]
>>> np.hsplit(a,3)
[array([1]), array([2]), array([3])]
>>> np.vsplit(c,2)
[array([[1.5, 2., 1. ],
       [4., 5., 6. ]]])
[array([[3., 2., 3.]])
       [4., 5., 6.]])
```

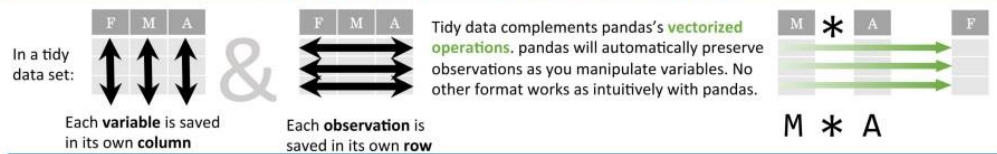
Permute array dimensions
Permute array dimensions
Flatten the array
Reshape, but don't change data
Return a new array with shape (2,6)
Append items to an array
Insert items in an array
Delete items from an array
Concatenate arrays
Stack arrays vertically (row-wise)
Stack arrays vertically (row-wise)
Stack arrays horizontally (column-wise)
Stack arrays horizontally (column-wise)
Create stacked column-wise arrays
Create stacked column-wise arrays
Split the array horizontally at the 3rd index
Split the array vertically at the 2nd index

DataCamp

Learn Python for Data Science Interactively



Tidy Data – A foundation for wrangling in pandas



Syntax – Creating DataFrames

| | a | b | c |
|---|---|---|----|
| 1 | 4 | 7 | 10 |
| 2 | 5 | 8 | 11 |
| 3 | 6 | 9 | 12 |

```
df = pd.DataFrame(
    {"a": [4, 5, 6],
     "b": [7, 8, 9],
     "c": [10, 11, 12]},
    index = [1, 2, 3])
```

Specify values for each column.

```
df = pd.DataFrame(
    [[4, 7, 10],
     [5, 8, 11],
     [6, 9, 12]],
    index=[1, 2, 3],
    columns=['a', 'b', 'c'])
```

Specify values for each row.

| n | v | a | b | c |
|---|---|---|---|----|
| d | 1 | 4 | 7 | 10 |
| e | 2 | 5 | 8 | 11 |
| e | 2 | 6 | 9 | 12 |

```
df = pd.DataFrame(
    {"a": [4, 5, 6],
     "b": [7, 8, 9],
     "c": [10, 11, 12]},
    index = pd.MultiIndex.from_tuples(
        [( 'd', 1), ('d', 2), ('e', 2)],
        names=['n', 'v']))
```

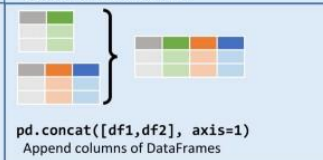
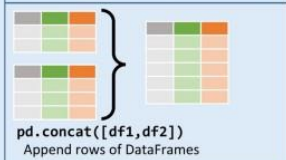
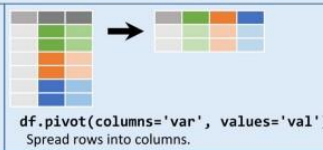
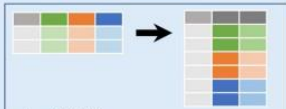
Create DataFrame with a MultiIndex

Method Chaining

Most pandas methods return a DataFrame so that another pandas method can be applied to the result. This improves readability of code.

```
df = (pd.melt(df)
      .rename(columns={
          'variable': 'var',
          'value': 'val'})
      .query('val >= 200'))
```

Reshaping Data – Change the layout of a data set



```
df.sort_values('mpg')
    Order rows by values of a column (low to high).

df.sort_values('mpg', ascending=False)
    Order rows by values of a column (high to low).

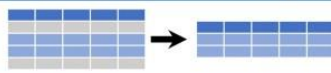
df.rename(columns = {'y': 'year'})
    Rename the columns of a DataFrame

df.sort_index()
    Sort the index of a DataFrame

df.reset_index()
    Reset index of DataFrame to row numbers, moving index to columns.

df.drop(['Length', 'Height'], axis=1)
    Drop columns from DataFrame
```

Subset Observations (Rows)



```
df[df.Length > 7]
    Extract rows that meet logical criteria.

df.sample(frac=0.5)
    Randomly select fraction of rows.

df.sample(n=10)
    Randomly select n rows.

df.iloc[10:20]
    Select rows by position.

df.nlargest(n, 'value')
    Select and order top n entries.

df.nsmallest(n, 'value')
    Select and order bottom n entries.
```

Subset Variables (Columns)



```
df[['width', 'length', 'species']]
    Select multiple columns with specific names.

df['width'] or df.width
    Select single column with specific name.

df.filter(regex='regex')
    Select columns whose name matches regular expression regex.
```

| | regex (Regular Expressions) | Examples |
|--------------------|--|----------|
| '\.' | Matches strings containing a period '.' | |
| 'Length\$' | Matches strings ending with word 'Length' | |
| '^Sepal' | Matches strings beginning with the word 'Sepal' | |
| '^x[1-5]\$' | Matches strings beginning with 'x' and ending with 1,2,3,4,5 | |
| '^(?!Species\$).*' | Matches strings except the string 'Species' | |

```
df.loc[:, 'x2': 'x4']
    Select all columns between x2 and x4 (inclusive).

df.iloc[:, [1, 2, 5]]
    Select columns in positions 1, 2 and 5 (first column is 0).

df.loc[df['a'] > 10, ['a', 'c']]
    Select rows meeting logical condition, and only the specific columns.
```

| Logic in Python (and pandas) | | |
|------------------------------|------------------------|--|
| < | Less than | != Not equal to |
| > | Greater than | df.column.isin(values) Group membership |
| == | Equals | pd.isnull(obj) Is NaN |
| <= | Less than or equals | pd.notnull(obj) Is not NaN |
| >= | Greater than or equals | &, , ~, ^, df.any(), df.all() Logical and, or, not, xor, any, all |

<http://pandas.pydata.org/> This cheat sheet inspired by RStudio Data Wrangling Cheatsheet (<https://www.rstudio.com/wp-content/uploads/2015/02/data-wrangling-cheat-sheet.pdf>) Written by Irv Lustin, Princeton Consultants

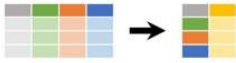
Summarize Data

df['w'].value_counts()
Count number of rows with each unique value of variable

len(df)
of rows in DataFrame.

df['w'].nunique()
of distinct values in a column.

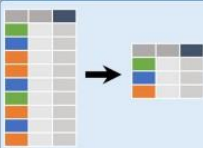
df.describe()
Basic descriptive statistics for each column (or GroupBy)



pandas provides a large set of **summary functions** that operate on different kinds of pandas objects (DataFrame columns, Series, GroupBy, Expanding and Rolling (see below)) and produce single values for each of the groups. When applied to a DataFrame, the result is returned as a pandas Series for each column. Examples:

| | |
|--|--|
| sum() Sum values of each object. | min() Minimum value in each object. |
| count() Count non-NA/null values of each object. | max() Maximum value in each object. |
| median() Median value of each object. | mean() Mean value of each object. |
| quantile([0.25, 0.75]) Quantiles of each object. | var() Variance of each object. |
| apply(function) Apply function to each object. | std() Standard deviation of each object. |

Group Data



df.groupby(by="col")
Return a GroupBy object, grouped by values in column named "col".

df.groupby(level="ind")
Return a GroupBy object, grouped by values in index level named "ind".

All of the summary functions listed above can be applied to a group. Additional GroupBy functions:

size()
Size of each group.

agg(function)
Aggregate group using function.

Handling Missing Data

df.dropna()
Drop rows with any column having NA/null data.

df.fillna(value)
Replace all NA/null data with value.

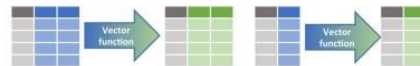
Make New Columns



df.assign(Area=lambda df: df.Length*df.Height)
Compute and append one or more new columns.

df['Volume'] = df.Length*df.Height*df.Depth
Add single column.

pd.qcut(df.col, n, labels=False)
Bin column into n buckets.



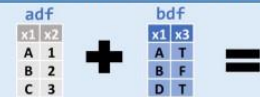
pandas provides a large set of **vector functions** that operate on all columns of a DataFrame or a single selected column (a pandas Series). These functions produce vectors of values for each of the columns, or a single Series for the individual Series. Examples:

| | |
|---|---|
| max(axis=1) Element-wise max. | min(axis=1) Element-wise min. |
| clip(lower=-10, upper=10) Trim values at input thresholds | abs() Absolute value. |

The examples below can also be applied to groups. In this case, the function is applied on a per-group basis, and the returned vectors are of the length of the original DataFrame.

| | |
|---|---|
| shift(1) Copy with values shifted by 1. | shift(-1) Copy with values lagged by 1. |
| rank(method='dense') Ranks with no gaps. | cumsum() Cumulative sum. |
| rank(method='min') Ranks. Ties get min rank. | cummax() Cumulative max. |
| rank(pct=True) Ranks rescaled to interval [0, 1]. | cummin() Cumulative min. |
| rank(method='first') Ranks. Ties go to first value. | cumprod() Cumulative product. |

Combine Data Sets



Standard Joins

pd.merge(adf, bdf, how='left', on='x1')
Join matching rows from bdf to adf.

pd.merge(adf, bdf, how='right', on='x1')
Join matching rows from adf to bdf.

pd.merge(adf, bdf, how='inner', on='x1')
Join data. Retain only rows in both sets.

pd.merge(adf, bdf, how='outer', on='x1')
Join data. Retain all values, all rows.

Filtering Joins

adf[adf.x1.isin(bdf.x1)]
All rows in adf that have a match in bdf.

adf[~adf.x1.isin(bdf.x1)]
All rows in adf that do not have a match in bdf.



Set-like Operations

pd.merge(ydf, zdf)
Rows that appear in both ydf and zdf (Intersection).

pd.merge(ydf, zdf, how='outer')
Rows that appear in either or both ydf and zdf (Union).

pd.merge(ydf, zdf, how='outer', indicator=True)
.query('_merge == "left_only"')
.drop(['_merge'], axis=1)
Rows that appear in ydf but not zdf (Setdiff).

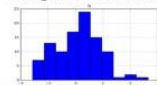
Windows

df.expanding()
Return an Expanding object allowing summary functions to be applied cumulatively.

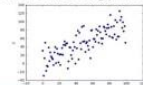
df.rolling(n)
Return a Rolling object allowing summary functions to be applied to windows of length n.

Plotting

df.plot.hist()
Histogram for each column



df.plot.scatter(x='w', y='h')
Scatter chart using pairs of points



Data Wrangling with dplyr and tidyr

Cheat Sheet



Tidy Data - A foundation for wrangling in R

In a tidy data set:

- Each **variable** is saved in its own **column**
- Each **observation** is saved in its own **row**

Tidy data complements R's **vectorized operations**. R will automatically preserve observations as you manipulate variables. No other format works as intuitively with R.




Syntax - Helpful conventions for wrangling

`dplyr::tbl_df(iris)`

Converts data to tbl class. tbl's are easier to examine than data frames. R displays only the data that fits onscreen:

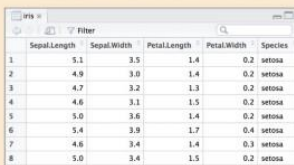
```
Source: local data frame [150 x 5]
  Sepal.Length Sepal.Width Petal.Length
1           5.1           3.5           1.4
2           4.9           3.0           1.4
3           4.7           3.2           1.3
4           4.6           3.1           1.5
5           5.0           3.6           1.4
..          ...           ...           ...
Variables not shown: Petal.Width (dbl),
Species (fctr)
```

`dplyr::glimpse(iris)`

Information dense summary of tbl data.

`utils::View(iris)`

View data set in spreadsheet-like display (note capital V).



`dplyr::%>%`


Passes object on left hand side as first argument (or . argument) of function on righthand side.

`x %>% f(y)` is the same as `f(x, y)`
`y %>% f(x, ., z)` is the same as `f(x, y, z)`

"Piping" with `%>%` makes code more readable, e.g.

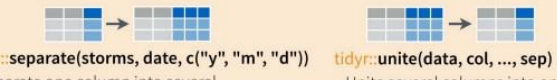
```
iris %>%
  group_by(Species) %>%
  summarise(avg = mean(Sepal.Width)) %>%
  arrange(avg)
```

Reshaping Data - Change the layout of a data set



`tidyr::gather(cases, "year", "n", 2:4)`
Gather columns into rows.

`tidyr::spread(pollution, size, amount)`
Spread rows into columns.



`tidyr::separate(storms, date, c("y", "m", "d"))`
Separate one column into several.

`tidyr::unite(data, col, ..., sep)`
Unite several columns into one.

`dplyr::data_frame(a = 1:3, b = 4:6)`
Combine vectors into data frame (optimized).

`dplyr::arrange(mtcars, mpg)`
Order rows by values of a column (low to high).

`dplyr::arrange(mtcars, desc(mpg))`
Order rows by values of a column (high to low).

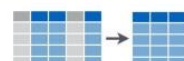
`dplyr::rename(tb, y = year)`
Rename the columns of a data frame.

Subset Observations (Rows)



- `dplyr::filter(iris, Sepal.Length > 7)`
Extract rows that meet logical criteria.
- `dplyr::distinct(iris)`
Remove duplicate rows.
- `dplyr::sample_frac(iris, 0.5, replace = TRUE)`
Randomly select fraction of rows.
- `dplyr::sample_n(iris, 10, replace = TRUE)`
Randomly select n rows.
- `dplyr::slice(iris, 10:15)`
Select rows by position.
- `dplyr::top_n(storms, 2, date)`
Select and order top n entries (by group if grouped data).

Subset Variables (Columns)



`dplyr::select(iris, Sepal.Width, Petal.Length, Species)`
Select columns by name or helper function.

Helper functions for select - ?select

- `select(iris, contains(" "))`
Select columns whose name contains a character string.
- `select(iris, ends_with("Length"))`
Select columns whose name ends with a character string.
- `select(iris, everything())`
Select every column.
- `select(iris, matches("t"))`
Select columns whose name matches a regular expression.
- `select(iris, num_range("x", 1:5))`
Select columns named x1, x2, x3, x4, x5.
- `select(iris, one_of(c("Species", "Genus")))`
Select columns whose names are in a group of names.
- `select(iris, starts_with("Sepal"))`
Select columns whose name starts with a character string.
- `select(iris, Sepal.Length:Petal.Width)`
Select all columns between Sepal.Length and Petal.Width (inclusive).
- `select(iris, -Species)`
Select all columns except Species.

| Logic in R - ?Comparison, ?base::Logic | | | |
|--|--------------------------|------------------------|-------------------|
| < | Less than | != | Not equal to |
| > | Greater than | %in% | Group membership |
| == | Equal to | is.na | Is NA |
| <= | Less than or equal to | !is.na | Is not NA |
| >= | Greater than or equal to | &, , !, xor, any, all | Boolean operators |

Summarise Data



dplyr::summarise(iris, avg = mean(Sepal.Length))

Summarise data into single row of values.

dplyr::summarise_each(iris, funs(mean))

Apply summary function to each column.

dplyr::count(iris, Species, wt = Sepal.Length)

Count number of rows with each unique value of variable (with or without weights).



Summarise uses **summary functions**, functions that take a vector of values and return a single value, such as:

dplyr::first

First value of a vector.

dplyr::last

Last value of a vector.

dplyr::nth

Nth value of a vector.

dplyr::n

of values in a vector.

dplyr::n_distinct

of distinct values in a vector.

IQR

IQR of a vector.

min

Minimum value in a vector.

max

Maximum value in a vector.

mean

Mean value of a vector.

median

Median value of a vector.

var

Variance of a vector.

sd

Standard deviation of a vector.

Group Data

dplyr::group_by(iris, Species)

Group data into rows with the same value of Species.

dplyr::ungroup(iris)

Remove grouping information from data frame.

iris %>% group_by(Species) %>% summarise(...)

Compute separate summary row for each group.



Make New Variables



dplyr::mutate(iris, sepal = Sepal.Length + Sepal.Width)

Compute and append one or more new columns.

dplyr::mutate_each(iris, funs(min_rank))

Apply window function to each column.

dplyr::transmute(iris, sepal = Sepal.Length + Sepal.Width)

Compute one or more new columns. Drop original columns.



Mutate uses **window functions**, functions that take a vector of values and return another vector of values, such as:

dplyr::lead

Copy with values shifted by 1.

dplyr::lag

Copy with values lagged by 1.

dplyr::dense_rank

Ranks with no gaps.

dplyr::min_rank

Ranks. Ties get min rank.

dplyr::percent_rank

Ranks rescaled to [0, 1].

dplyr::row_number

Ranks. Ties got to first value.

dplyr::ntile

Bin vector into n buckets.

dplyr::between

Are values between a and b?

dplyr::cume_dist

Cumulative distribution.

dplyr::cumall

Cumulative **all**

dplyr::cumany

Cumulative **any**

dplyr::cummean

Cumulative **mean**

cumsum

Cumulative **sum**

cummax

Cumulative **max**

cummin

Cumulative **min**

cumprod

Cumulative **prod**

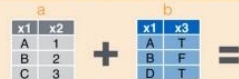
pmax

Element-wise **max**

pmin

Element-wise **min**

Combine Data Sets



Mutating Joins

| x1 | x2 | x3 |
|----|----|----|
| A | 1 | T |
| B | 2 | F |
| C | 3 | NA |

dplyr::left_join(a, b, by = "x1")
Join matching rows from b to a.

| x1 | x2 | x3 |
|----|----|----|
| A | T | 1 |
| B | F | 2 |
| D | T | NA |

dplyr::right_join(a, b, by = "x1")
Join matching rows from a to b.

| x1 | x2 | x3 |
|----|----|----|
| A | 1 | T |
| B | 2 | F |

dplyr::inner_join(a, b, by = "x1")
Join data. Retain only rows in both sets.

| x1 | x2 | x3 |
|----|----|----|
| A | 1 | T |
| C | 3 | NA |
| D | NA | T |

dplyr::full_join(a, b, by = "x1")
Join data. Retain all values, all rows.

Filtering Joins

| x1 | x2 |
|----|----|
| A | 1 |
| B | 2 |

dplyr::semi_join(a, b, by = "x1")
All rows in a that have a match in b.

| x1 | x2 |
|----|----|
| C | 3 |

dplyr::anti_join(a, b, by = "x1")
All rows in a that do not have a match in b.



Set Operations

| x1 | x2 |
|----|----|
| B | 2 |
| C | 3 |

dplyr::intersect(y, z)
Rows that appear in both y and z.

| x1 | x2 |
|----|----|
| A | 1 |
| B | 2 |
| C | 3 |
| D | 4 |

dplyr::union(y, z)
Rows that appear in either or both y and z.

| x1 | x2 |
|----|----|
| A | 1 |

dplyr::setdiff(y, z)
Rows that appear in y but not z.

Binding

| x1 | x2 |
|----|----|
| A | 1 |
| B | 2 |
| C | 3 |
| D | 4 |

dplyr::bind_rows(y, z)
Append z to y as new rows.

| x1 | x2 | x1 | x2 |
|----|----|----|----|
| A | 1 | B | 2 |
| B | 2 | C | 3 |
| C | 3 | D | 4 |

dplyr::bind_cols(y, z)
Append z to y as new columns.
Caution: matches rows by position.

Python For Data Science Cheat Sheet

SciPy - Linear Algebra

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SciPy

The SciPy library is one of the core packages for scientific computing that provides mathematical algorithms and convenience functions built on the NumPy extension of Python.



Interacting With NumPy

Also see NumPy

```
>>> import numpy as np
>>> a = np.array([1,2,3])
>>> b = np.array([[1+5j,2j,3j], (4j,5j,6j)])
>>> c = np.array([[1.5,2.3], (4,5,6)], [(3,2,1), (4,5,6)])
```

Index Tricks

```
>>> np.mgrid[0:5,0:5] Create a dense meshgrid
>>> np.ogrid[0:2,0:2] Create an open meshgrid
>>> np.r_[3,0]+5,-1:1:10j Stack arrays vertically (row-wise)
>>> np.c_[b,c] Create stacked column-wise arrays
```

Shape Manipulation

```
>>> np.transpose(b) Permute array dimensions
>>> b.flatten() Flatten the array
>>> np.hstack((b,c)) Stack arrays horizontally (column-wise)
>>> np.vstack((a,b)) Stack arrays vertically (row-wise)
>>> np.hsplit(c,2) Split the array horizontally at the 2nd index
>>> np.vsplit(d,2) Split the array vertically at the 2nd index
```

Polynomials

```
>>> from numpy import poly1d
>>> p = poly1d([3,4,5]) Create a polynomial object
```

Vectorizing Functions

```
>>> def myfunc(a):
    if a < 0:
        return a**2
    else:
        return a/2
>>> np.vectorize(myfunc) Vectorize functions
```

Type Handling

```
>>> np.real(b) Return the real part of the array elements
>>> np.imag(b) Return the imaginary part of the array elements
>>> np.real_if_close(c,tol=1000) Return a real array if complex parts close to 0
>>> np.cast['*f'](np.pi) Cast object to a data type
```

Other Useful Functions

```
>>> np.angle(b,deg=True) Return the angle of the complex argument
>>> g = np.linspace(0,np.pi,num=5) Create an array of evenly spaced values
>>> g[3] += np.pi (number of samples)
>>> np.unwrap(g) Unwrap
>>> np.logspace(0,10,3) Create an array of evenly spaced values (log scale)
>>> np.select([c<4],[c+2]) Return values from a list of arrays depending on conditions
>>> misc.factorial(a) Factorial
>>> misc.comb(10,3,exact=True) Combine N things taken at k time
>>> misc.central_diff_weights(3) Weights for Np-point central derivative
>>> misc.derivative(myfunc,1.0) Find the n-th derivative of a function at a point
```

Linear Algebra

You'll use the `linalg` and `sparse` modules. Note that `scipy.linalg` contains and expands on `numpy.linalg`.

Also see NumPy

```
>>> from scipy import linalg, sparse
```

Creating Matrices

```
>>> A = np.matrix(np.random.random((2,2)))
>>> B = np.asmatrix(b)
>>> C = np.mat(np.random.random((10,5)))
>>> D = np.mat([[13,4], [5,6]])
```

Basic Matrix Routines

```
Inverse
>>> linalg.inv(A) Inverse Inverse
>>> A.T Transpose matrix Transpose matrix
>>> A.H Conjugate transpose Conjugate transpose

Trace
>>> np.trace(A) Trace Trace

Norm
>>> linalg.norm(A) Frobenius norm Frobenius norm
>>> linalg.norm(A,1) L1 norm (max column sum) L1 norm (max column sum)
>>> linalg.norm(A,np.inf) L1 norm (max row sum) L1 norm (max row sum)

Rank
>>> np.linalg.matrix_rank(C) Matrix rank Matrix rank

Determinant
>>> linalg.det(A) Determinant Determinant

Solving linear problems
>>> linalg.solve(A,b) Solver for dense matrices Solver for dense matrices
>>> E = np.mat(A.T) Solver for dense matrices Solver for dense matrices
>>> linalg.lstsq(F,E) Least-squares solution to linear matrix equation Least-squares solution to linear matrix equation

Generalized inverse
>>> linalg.pinv(C) Compute the pseudo-inverse of a matrix (least-squares solver) Compute the pseudo-inverse of a matrix (SVD)
>>> linalg.pinv2(C) Compute the pseudo-inverse of a matrix (SVD) Compute the pseudo-inverse of a matrix (SVD)
```

Creating Sparse Matrices

```
>>> F = np.eye(3, k=1) Create a 2x2 identity matrix Create a 2x2 identity matrix
>>> G = np.mat(np.identity(2)) Create a 2x2 identity matrix Create a 2x2 identity matrix
>>> C[C > 0.5] = 0
>>> H = sparse.csr_matrix(C) Compressed Sparse Row matrix Compressed Sparse Row matrix
>>> T = sparse.csc_matrix(D) Compressed Sparse Column matrix Compressed Sparse Column matrix
>>> J = sparse.dok_matrix(A) Dictionary Of Keys matrix Dictionary Of Keys matrix
>>> E.todense() Sparse matrix to full matrix Sparse matrix to full matrix
>>> sparse.isspmatrix_csc(A) Identify sparse matrix Identify sparse matrix
```

Sparse Matrix Routines

```
Inverse
>>> sparse.linalg.inv(I) Inverse Inverse

Norm
>>> sparse.linalg.norm(I) Norm Norm

Solving linear problems
>>> sparse.linalg.spsolve(H,I) Solver for sparse matrices Solver for sparse matrices
```

Sparse Matrix Functions

```
>>> sparse.linalg.expm(I) Sparse matrix exponential Sparse matrix exponential
```

Asking For Help

```
>>> help(scipy.linalg.diagsvd)
>>> np.info(np.matrix)
```

Matrix Functions

```
Addition
>>> np.add(A,D) Addition Addition

Subtraction
>>> np.subtract(A,D) Subtraction Subtraction

Division
>>> np.divide(A,D) Division Division

Multiplication
>>> A @ B Multiplication operator (Python 3) Multiplication operator
>>> np.multiply(D,A) Multiplication Multiplication
>>> np.dot(A,D) Vector dot product Vector dot product
>>> np.vdot(A,D) Inner product Inner product
>>> np.outer(A,D) Outer product Outer product
>>> np.tensordot(A,D) Tensor dot product Tensor dot product
>>> np.kron(A,D) Kronecker product Kronecker product

Exponential Functions
>>> linalg.expm(A) Matrix exponential Matrix exponential
>>> linalg.expm2(A) Matrix exponential (Taylor Series) Matrix exponential (Taylor Series)
>>> linalg.expm3(D) Matrix exponential (eigenvalue decomposition) Matrix exponential (eigenvalue decomposition)

Logarithm Function
>>> linalg.logm(A) Matrix logarithm Matrix logarithm

Trigonometric Functions
>>> linalg.sinm(D) Matrix sine Matrix sine
>>> linalg.cosm(D) Matrix cosine Matrix cosine
>>> linalg.tanm(A) Matrix tangent Matrix tangent

Hyperbolic Trigonometric Functions
>>> linalg.sinhm(D) Hyperbolic matrix sine Hyperbolic matrix sine
>>> linalg.coshm(D) Hyperbolic matrix cosine Hyperbolic matrix cosine
>>> linalg.tanhm(A) Hyperbolic matrix tangent Hyperbolic matrix tangent

Matrix Sign Function
>>> np.signm(A) Matrix sign function Matrix sign function

Matrix Square Root
>>> linalg.sqrtm(A) Matrix square root Matrix square root

Arbitrary Functions
>>> linalg.funm(A, lambda x: x**x) Evaluate matrix function Evaluate matrix function
```

Decompositions

```
Eigenvalues and Eigenvectors
>>> la, v = linalg.eig(A) Solve ordinary or generalized eigenvalue problem for square matrix Solve ordinary or generalized eigenvalue problem for square matrix
>>> l1, l2 = la Unpack eigenvalues Unpack eigenvalues
>>> v[:,0] First eigenvector First eigenvector
>>> v[:,1] Second eigenvector Second eigenvector
>>> linalg.eigvals(A) Unpack eigenvalues Unpack eigenvalues

Singular Value Decomposition
>>> U, s, Vh = linalg.svd(B) Singular Value Decomposition (SVD) Singular Value Decomposition (SVD)
>>> M, N = B.shape Construct sigma matrix in SVD Construct sigma matrix in SVD
>>> Sig = linalg.diagsvd(s,M,N) Construct sigma matrix in SVD Construct sigma matrix in SVD

LU Decomposition
>>> P, L, U = linalg.lu(C) LU Decomposition LU Decomposition
```

Sparse Matrix Decompositions

```
>>> la, v = sparse.linalg.eigs(F,1) Eigenvalues and eigenvectors Eigenvalues and eigenvectors
>>> sparse.linalg.svds(H, 2) SVD SVD
```

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Python For Data Science Cheat Sheet

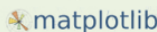
Matplotlib

Learn Python Interactively at www.datacamp.com



Matplotlib

Matplotlib is a Python 2D plotting library which produces publication-quality figures in a variety of hardcopy formats and interactive environments across platforms.



1 Prepare The Data

Also see Lists & NumPy

```
1D Data
>>> import numpy as np
>>> x = np.linspace(0, 100, 100)
>>> y = np.cos(x)
>>> z = np.sin(x)

2D Data or Images
>>> data = 2 * np.random.random((10, 10))
>>> data2 = 3 * np.random.random((10, 10))
>>> Y, X = np.mgrid[-3:3:100j, -3:3:100j]
>>> U = -1 * X**2 + Y
>>> from matplotlib.cbook import get_sample_data
>>> img = np.load(get_sample_data('axes_grid/bivariate_normal.npy'))
```

2 Create Plot

```
>>> import matplotlib.pyplot as plt
>>> fig = plt.figure()
>>> fig2 = plt.figure(figsize=plt.figaspect(2.0))
>>> ax = fig.add_subplot(2,1,1)
>>> ax1 = fig.add_subplot(221) # row-col-num
>>> ax3 = fig.add_subplot(212)
>>> fig3, axes = plt.subplots(nrows=2,ncols=2)
>>> fig4, axes2 = plt.subplots(ncols=3)
```

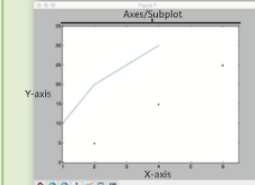
3 Plotting Routines

```
1D Data
>>> fig, ax = plt.subplots()
>>> lines = ax.plot(x,y) Draw points with lines or markers connecting them
>>> ax.scatter(x,y) Draw unconnected points, scaled or colored
>>> axes[0,0].bar([1,2,3],[3,4,5]) Plot vertical rectangles (constant width)
>>> axes[1,0].barh([0.5,1,2.5],[0,1,2]) Plot horizontal rectangles (constant height)
>>> axes[1,1].axhline(0.45) Draw a horizontal line across axes
>>> axes[0,1].axvline(0.65) Draw a vertical line across axes
>>> ax.fill(x,y,color='blue') Draw filled polygons
>>> ax.fill_between(x,y,color='yellow') Fill between y-values and 0

2D Data or Images
>>> fig, ax = plt.subplots()
>>> im = ax.imshow(img, cmap='gist_earth', interpolation='nearest', vmin=-4, vmax=2) Colormapped or RGB arrays
```

Plot Anatomy & Workflow

Plot Anatomy



Workflow

The basic steps to creating plots with matplotlib are:

- 1 Prepare data
- 2 Create plot
- 3 Plot
- 4 Customize plot
- 5 Save plot
- 6 Show plot

4 Customize Plot

```
Colors, Color Bars & Color Maps
>>> plt.plot(x, x, x, x**2, x, x**3)
>>> ax.plot(x, y, alpha=0.4)
>>> ax.plot(x, y, c='k')
>>> fig.colorbar(img, orientation='horizontal')
>>> im = ax.imshow(img, cmap='seismic')

Markers
>>> fig, ax = plt.subplots()
>>> ax.scatter(x,y,marker=".")
>>> ax.plot(x,y,marker="o")

Linestyles
>>> plt.plot(x,y,linewidth=4.0)
>>> plt.plot(x,y,ls='solid')
>>> plt.plot(x,y,ls='--')
>>> plt.plot(x,y,'--',x**2,y**2,'-.')
>>> plt.setp(lines,color='r',linewidth=4.0)

Text & Annotations
>>> ax.text(1, 2, 'Example Graph', style='italic')
>>> ax.annotate("Sine", xy=(8, 0), xycoords='data', xytext=(10.5, 0), textcoords='data', arrowprops=dict(arrowstyle="->", connectionstyle="arc3"),)
```

Mathtext

```
>>> plt.title(r'$\sigma_i=15\$', fontsize=20)
```

Limits, Legends & Layouts

```
Limits & Autoscaling
>>> ax.margins(x=0,y=0.1) Add padding to a plot
>>> ax.axis('equal') Set the aspect ratio of the plot to 1
>>> ax.set_xlim([0,10.5],ylim=[-1.5,1.5]) Set limits for x and y-axis
>>> ax.set_ylim(0,10.5) Set limits for x-axis

Legends
>>> ax.set(title='An Example Axes', ylabel='Y-Axis', xlabel='X-Axis') Set a title and x and y-axis labels

No overlapping plot elements
>>> ax.legend(loc='best')

Manually set x-ticks
>>> ax.xaxis.set(ticks=range(1,5), ticklabel=[3,100,-12,"foo"]) Make y-ticks longer and go in and out

Adjust the spacing between subplots
>>> ax.tick_params(axis='y', direction='inout', length=10)
>>> fig.tight_layout() Fit subplot(s) in to the figure area

Axis Spines
>>> ax1.spines['top'].set_visible(False) Make the top axis line for a plot invisible
>>> ax1.spines['bottom'].set_position(('outward',10)) Move the bottom axis line outward
```

5 Save Plot

```
Save figures
>>> plt.savefig('foo.png')
Save transparent figures
>>> plt.savefig('foo.png', transparent=True)
```

6 Show Plot

```
>>> plt.show()
```

Close & Clear

```
>>> plt.cla() Clear an axis
>>> plt.clf() Clear the entire figure
>>> plt.close() Close a window
```

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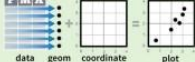
Data Visualization with ggplot2

Cheat Sheet



Basics

ggplot2 is based on the **grammar of graphics**, the idea that you can build every graph from the same few components: a **data** set, a set of **geoms**—visual marks that represent data points, and a **coordinate system**.



To display data values, map variables in the data set to aesthetic properties of the geom like **size**, **color**, and **x** and **y** locations.



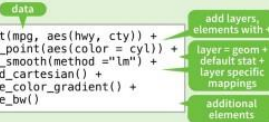
Build a graph with `qplot()` or `ggplot()`

aesthetic mappings data geom

`qplot(x = cty, y = hwy, color = cyl, data = mpg, geom = "point")`
Creates a complete plot with given data, geom, and mappings. Supplies many useful defaults.

`ggplot(data = mpg, aes(x = cty, y = hwy))`

Begins a plot that you finish by adding layers to. No defaults, but provides more control than `qplot()`.



Add a new layer to a plot with a `geom_*()` or `stat_*()` function. Each provides a geom, a set of aesthetic mappings, and a default stat and position adjustment.

`last_plot()`

Returns the last plot

`ggsave("plot.png", width = 5, height = 5)`

Saves last plot as 5" x 5" file named "plot.png" in working directory. Matches file type to file extension.

Geoms - Use a geom to represent data points, use the geom's aesthetic properties to represent variables. Each function returns a layer.

One Variable

Continuous

`a <- ggplot(mpg, aes(hwy))`

a + `geom_area(stat = "bin")`

x, y, alpha, color, fill, linetype, size

b + `geom_area(aes(y = ..density..), stat = "bin")`

a + `geom_density(kernel = "gaussian")`

x, y, alpha, color, fill, linetype, size, weight

b + `geom_density(aes(y = ..county..))`

a + `geom_dotplot()`

x, y, alpha, color, fill

a + `geom_freqpoly()`

x, y, alpha, color, linetype, size

b + `geom_freqpoly(aes(y = ..density..))`

a + `geom_histogram(binwidth = 5)`

x, y, alpha, color, fill, linetype, size, weight

b + `geom_histogram(aes(y = ..density..))`

Discrete

`b <- ggplot(mpg, aes(class))`

b + `geom_bar()`

x, alpha, color, fill, linetype, size, weight

Graphical Primitives

`c <- ggplot(map, aes(long, lat))`

c + `geom_polygon(aes(group = group))`

x, y, alpha, color, fill, linetype, size

`d <- ggplot(economics, aes(date, unemploy))`

d + `geom_path(lineend = "butt", linejoin = "round", linemitre = 1)`

x, y, alpha, color, linetype, size

d + `geom_ribbon(aes(ymin = unemploy - 900, ymax = unemploy + 900))`

x, ymax, ymin, alpha, color, fill, linetype, size

`e <- ggplot(seals, aes(x = long, y = lat))`

e + `geom_segment(aes(xend = long + delta_long, yend = lat + delta_lat))`

x, xend, y, yend, alpha, color, linetype, size

e + `geom_rect(aes(xmin = long, ymin = lat, xmax = long + delta_long, ymax = lat + delta_lat))`

xmax, xmin, ymax, ymin, alpha, color, fill, linetype, size

Two Variables

Continuous X, Continuous Y

`f <- ggplot(mpg, aes(cty, hwy))`

f + `geom_blank()`

x, y, alpha, color, fill, shape, size

f + `geom_jitter()`

x, y, alpha, color, fill, shape, size

f + `geom_point()`

x, y, alpha, color, fill, shape, size

f + `geom_quantile()`

x, y, alpha, color, linetype, size, weight

f + `geom_rug(sides = "bl")`

alpha, color, linetype, size

f + `geom_smooth(model = lm)`

x, y, alpha, color, fill, linetype, size, weight

f + `geom_text(aes(label = cty))`

x, y, label, alpha, angle, color, family, fontface, hjust, lineheight, size, vjust

Discrete X, Continuous Y

`g <- ggplot(mpg, aes(class, hwy))`

g + `geom_bar(stat = "identity")`

x, y, alpha, color, fill, linetype, size, weight

g + `geom_boxplot()`

lower, middle, upper, x, ymax, ymin, alpha, color, fill, linetype, shape, size, weight

g + `geom_dotplot(binaxis = "y", stackdir = "center")`

x, y, alpha, color, fill

g + `geom_violin(scale = "area")`

x, y, alpha, color, fill, linetype, size, weight

Discrete X, Discrete Y

`h <- ggplot(diamonds, aes(cut, color))`

h + `geom_jitter()`

x, y, alpha, color, fill, shape, size

Continuous Bivariate Distribution

`i <- ggplot(movies, aes(year, rating))`

i + `geom_bin2d(binwidth = c(5, 0.5))`

xmax, xmin, ymax, ymin, alpha, color, fill, linetype, size, weight

i + `geom_density2d()`

x, y, alpha, color, fill, linetype, size

i + `geom_hex()`

x, y, alpha, color, fill, size

Continuous Function

`j <- ggplot(economics, aes(date, unemploy))`

j + `geom_area()`

x, y, alpha, color, fill, linetype, size

j + `geom_line()`

x, y, alpha, color, linetype, size

j + `geom_step(direction = "hv")`

x, y, alpha, color, linetype, size

Visualizing error

`df <- data.frame(grp = c("A", "B"), fit = 4:5, se = 1:2)`

`k <- ggplot(df, aes(grp, fit, ymin = fit-se, ymax = fit+se))`

k + `geom_crossbar(fatten = 2)`

x, y, ymax, ymin, alpha, color, fill, linetype, size

k + `geom_errorbar()`

x, ymax, ymin, alpha, color, linetype, size, width (also `geom_errorbarh()`)

k + `geom_linerange()`

x, ymin, ymax, alpha, color, linetype, size

k + `geom_pointrange()`

x, y, ymin, ymax, alpha, color, fill, linetype, shape, size

Maps

`data <- data.frame(murder = USArrests$Murder, state = tolower(rownames(USArrests)))`

`map <- map_data("state")`

`l <- ggplot(data, aes(fill = murder))`

l + `geom_map(aes(map_id = state), map = map) +`

`expand_limits(x = map$long, y = map$lat)`

map_id, alpha, color, fill, linetype, size

Three Variables

`seals$z <- with(seals, sqrt(delta_long^2 + delta_lat^2))`

`m <- ggplot(seals, aes(long, lat))`

m + `geom_raster(aes(fill = z), hjust=0.5, vjust=0.5, interpolate=FALSE)`

x, y, alpha, fill

m + `geom_tile(aes(fill = z))`

x, y, z, alpha, color, fill, linetype, size, weight

m + `geom_contour(aes(z = z))`

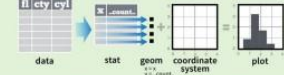
x, y, z, alpha, color, fill, linetype, size, weight

m + `geom_tile(aes(fill = z))`

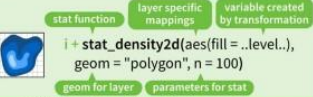
x, y, alpha, color, fill, linetype, size

Stats - An alternative way to build a layer

Some plots visualize a **transformation** of the original data set. Use a **stat** to choose a common transformation to visualize, e.g. `a + geom_bar(stat = "bin")`



Each stat creates additional variables to map aesthetics to. These variables use a common `..name..` syntax. `stat` functions and `geom` functions both combine a `stat` with a `geom` to make a layer, i.e. `stat_bin(geom="bar")` does the same as `geom_bar(stat="bin")`



```

i + stat_density2d(aes(fill = ..level..),
  geom = "polygon", n = 100)
  
```

```

a + stat_bin(binwidth = 1, origin = 1)
x, y | ..count.., ..ncount.., ..density..
a + stat_bin2d(binwidth = 1, binaxis = "x")
x, y | ..count.., ..ncount..
a + stat_bin2d(adjust = 1, kernel = "gaussian")
x, y | ..count.., ..density.., ..scaled..
  
```

```

f + stat_bin2d(bins = 30, drop = TRUE)
x, y, fill | ..count.., ..density..
f + stat_binhex(bins = 30)
x, y, fill | ..count.., ..density..
f + stat_density2d(contour = TRUE, n = 100)
x, y, color, size | ..level..
  
```

```

m + stat_contour(aes(z = z))
x, y, z, order | ..level..
m + stat_spoke(aes(radius = z, angle = z))
angle, radius, x, yend | ..x.., ..xend.., ..y.., ..yend..
m + stat_summary_hex(aes(z = z), bins = 30, fun = mean)
x, y, z, fill | ..value..
m + stat_summary2d(aes(z = z), bins = 30, fun = mean)
x, y, z, fill | ..value..
  
```

```

g + stat_boxplot(coef = 1.5)
x, y | ..lower.., ..middle.., ..upper.., ..outliers..
g + stat_ydensity(adjust = 1, kernel = "gaussian", scale = "area")
x, y | ..density.., ..scaled.., ..count.., ..n.., ..violinwidth.., ..width..
  
```

```

f + stat_ecdf(n = 40)
x, y | ..x.., ..y..
f + stat_quantile(quantiles = c(0.25, 0.5, 0.75), formula = y ~ log(x),
  method = "rq")
x, y | ..quartile.., ..x.., ..y..
f + stat_smooth(method = "auto", formula = y ~ x, se = TRUE, n = 80,
  fullrange = FALSE, level = 0.95)
x, y | ..se.., ..x.., ..y.., ..ymin.., ..ymax..
  
```

```

ggplot() + stat_function(aes(x = -3:3),
  fun = dnorm, n = 101, args = list(sd=0.5))
x | ..y..
  
```

```

f + stat_identity()
ggplot() + stat_qq(aes(sample=1:100), distribution = qt,
  dparams = list(df=5))
sample, x, y | ..x.., ..y..
f + stat_sum()
x, y, size | ..size..
f + stat_summary(fun.data = "mean_cl_boot")
f + stat_uniq()
  
```

Scales

Scales control how a plot maps data values to the visual values of an aesthetic. To change the mapping, add a custom scale.



```

n <- b + geom_bar(aes(fill = fill))
  
```

Scale: `scale_fill_manual(values = c("skyblue", "royalblue", "blue", "navy"), limits = c("d", "e", "p", "r"), breaks = c("D", "E", "P", "R"), name = "fuel", labels = c("D", "E", "P", "R"))`

```

scale_*_continuous() - map cont' values to visual values
scale_*_discrete() - map discrete values to visual values
scale_*_identity() - use data values as visual values
scale_*_manual(values = c()) - map discrete values to manually chosen visual values
  
```

```

X and Y location scales
  
```

Use with x or y aesthetics (x shown here)

```

scale_x_date(labels = date_format("%m/%d"),
  breaks = date_breaks("2 weeks")) - treat x values as dates. See ?strptime for label formats.
scale_x_datetime() - treat x values as date times. Use same arguments as scale_x_date().
scale_x_log10() - Plot x on log10 scale
scale_x_reverse() - Reverse direction of x axis
scale_x_sqrt() - Plot x on square root scale
  
```

Color and fill scales

```

Discrete
n <- b + geom_bar(aes(fill = fill))
  
```

Continuous

```

o <- a + geom_dotplot(aes(fill = ..x..))
  
```

Manual shape values

```

p <- f + geom_point(aes(shape = fill))
  
```

```

n + scale_fill_brewer(palette = "Blues")
For palette choices: library(RColorBrewer); display.brewer.all()
n + scale_fill_grey(start = 0.2, end = 0.8, na.value = "red")
  
```

```

Shape scales
Manual shape values
p <- f + geom_point(aes(shape = fill))
  
```

```

Size scales
q <- f + geom_point(aes(size = cyl))
  
```

Coordinate Systems

```

r <- b + geom_bar()
xlim, ylim
  
```

The default cartesian coordinate system

```

r + coord_cartesian(xlim = c(0, 5))
  
```

Cartesian coordinates with fixed aspect ratio between x and y units

```

r + coord_fixed(ratio = 1/2)
  
```

Flipped Cartesian coordinates

```

r + coord_flip()
  
```

Polar coordinates

```

r + coord_polar(theta = "x", direction = 1)
  
```

Transformed cartesian coordinates. Set extras and strains to the name of a window function.

```

r + coord_trans(ytrans = "sqrt")
  
```

```

z + coord_map(projection = "ortho",
  orientation=c(41, -74, 0))
  
```

```

Position Adjustments
  
```

Position adjustments determine how to arrange geoms that would otherwise occupy the same space.

```

s <- ggplot(mpg, aes(fl, fill = drv))
  
```

```

s + geom_bar(position = "dodge")
s + geom_bar(position = "fill")
s + geom_bar(position = "stack")
f + geom_point(position = "jitter")
  
```

```

Themes
  
```

```

r + theme_bw()
r + theme_classic()
r + theme_grey()
r + theme_minimal()
  
```

```

ggthemes - Package with additional ggplot2 themes
  
```

Faceting

Facets divide a plot into subplots based on the values of one or more discrete variables.

```

t <- ggplot(mpg, aes(cty, hwy)) + geom_point()
  
```

```

t + facet_grid(~ fl)
t + facet_grid(year ~ .)
t + facet_grid(year ~ fl)
t + facet_wrap(~ fl)
  
```

```

Set scales to let axis limits vary across facets
t + facet_grid(y ~ x, scales = "free")
  
```

```

Set labeller to adjust facet labels
t + facet_grid(. ~ fl, labeller = label_both)
t + facet_grid(. ~ fl, labeller = label_quote(alpha ^ (.)))
t + facet_grid(. ~ fl, labeller = label_parsed)
  
```

Labels

```

t + ggtitle("New Plot Title")
t + xlab("New X label")
t + ylab("New Y label")
t + labs(title = "New title", x = "New x", y = "New y")
  
```

Legends

```

t + theme(legend.position = "bottom")
t + guides(color = "none")
t + scale_fill_discrete(name = "Title", labels = c("A", "B", "C"))
  
```

Zooming

```

Without clipping (preferred)
t + coord_cartesian(xlim = c(0, 100), ylim = c(10, 20))
  
```

```

With clipping (removes unseen data points)
t + xlim(0, 100) + ylim(10, 20)
t + scale_x_continuous(limits = c(0, 100)) +
  scale_y_continuous(limits = c(0, 100))
  
```


Python For Data Science Cheat Sheet

PySpark Basics

Learn Python for data science interactively at www.DataCamp.com



Spark

PySpark is the Spark Python API that exposes the Spark programming model to Python



Initializing Spark

SparkContext

```
>>> from pyspark import SparkContext
>>> sc = SparkContext(master = 'local[2]')
```

Inspect SparkContext

```
>>> sc.version
>>> sc.pythonVer
>>> sc.master
>>> str(sc.sparkHome)
>>> str(sc.sparkUser())
>>> sc.appName
>>> sc.applicationId
>>> sc.defaultParallelism
>>> sc.defaultMinPartitions
```

Retrieve SparkContext version
Retrieve Python version
Master URL to connect to
Path where Spark is installed on worker nodes
Retrieve name of the Spark User running SparkContext
Return application name
Retrieve application ID
Return default level of parallelism
Default minimum number of partitions for RDDs

Configuration

```
>>> from pyspark import SparkConf, SparkContext
>>> conf = SparkConf()
>>> conf.setMaster("local")
>>> conf.setAppName("My app")
>>> conf.set("spark.executor.memory", "1g")
>>> sc = SparkContext(conf = conf)
```

Using The Shell

In the PySpark shell, a special interpreter-aware SparkContext is already created in the variable called `sc`.

```
$ ./bin/spark-shell --master local[2]
$ ./bin/pyspark --master local[4] --py-files code.py
```

Set which master the context connects to with the `--master` argument, and add Python `.zip`, `.egg` or `.py` files to the runtime path by passing a comma-separated list to `--py-files`.

Loading Data

Parallelized Collections

```
>>> rdd = sc.parallelize(['a','b','c'])
>>> rdd2 = sc.parallelize(['a','b','c'], ('a',2), ('b',1))
>>> rdd3 = sc.parallelize(range(100))
>>> rdd4 = sc.parallelize(['a','b','c'], ('a','m','m','m'), ('b','m','m','m'))
```

External Data

Read either one text file from HDFS, a local file system or any Hadoop-supported file system URI with `textFile()`, or read in a directory of text files with `wholeTextFiles()`.

```
>>> textFile = sc.textFile("my/directory/*.txt")
>>> textFile2 = sc.wholeTextFiles("my/directory/*")
```

Retrieving RDD Information

Basic Information

```
>>> rdd.getNumPartitions()
>>> rdd.count()
>>> rdd.countByKey()
>>> rdd.countByValue()
>>> rdd.collectAsMap()
>>> rdd3.sum()
>>> sc.parallelize().isEmpty()
```

List the number of partitions
Count RDD instances
Count RDD instances by key
Count RDD instances by value
Return (key,value) pairs as a dictionary
Sum of RDD elements
Check whether RDD is empty

Summary

```
>>> rdd3.max()
>>> rdd3.min()
>>> rdd3.mean()
>>> rdd3.stdev()
>>> rdd3.variance()
>>> rdd3.histogram()
>>> rdd3.stats()
```

Maximum value of RDD elements
Minimum value of RDD elements
Mean value of RDD elements
Standard deviation of RDD elements
Compute variance of RDD elements
Compute histogram by bins
Summary statistics (count, mean, stdev, max & min)

Applying Functions

```
>>> rdd.map(lambda x: x*(x[1],x[0]))
>>> rdd5 = rdd.flatMap(lambda x: x*(x[1],x[0]))
>>> rdd5.collect()
>>> rdd4.flatMapValues(lambda x: x)
>>> rdd4.collect()
```

Apply a function to each RDD element
Apply a function to each RDD element and flatten the result
Apply a flatMap function to each (key,value) pair of rdd4 without changing the keys

Selecting Data

Getting

```
>>> rdd.collect()
>>> rdd.take(2)
>>> rdd.first()
>>> rdd.top(2)
```

Return a list with all RDD elements
Take first 2 RDD elements
Take first RDD element
Take top 2 RDD elements

Sampling

```
>>> rdd3.sample(False, 0.15, 81).collect()
```

Return sampled subset of rdd3

Filtering

```
>>> rdd.filter(lambda x: "a" in x)
>>> rdd5.distinct().collect()
>>> rdd.keys().collect()
```

Filter the RDD
Return distinct RDD values
Return (key,value) RDD's keys

Iterating

```
>>> def f(x): print(x)
>>> rdd.foreach(f)
>>> ('b', 2)
>>> ('a', 2)
```

Apply a function to all RDD elements

Reshaping Data

Reducing

```
>>> rdd.reduceByKey(lambda x,y: x+y)
>>> rdd.reduce(lambda a, b: a + b)
```

Merge the rdd values for each key
Merge the rdd values

Grouping by

```
>>> rdd3.groupBy(lambda x: x % 2)
>>> rdd.groupByKey()
>>> rdd.groupBy(lambda x: x*(x[1],x[0]))
```

Return RDD of grouped values
Group rdd by key

Aggregating

```
>>> seqOp = (lambda x,y: x(0)+y,x[1]+1)
>>> combOp = (lambda x,y: x(0)+y(0),x[1]+y(1))
>>> rdd3.aggregate((0,0),seqOp,combOp)
>>> rdd3.aggregateByKey((0,0),seqOp,combOp)
>>> rdd3.fold(0,add)
>>> rdd.foldByKey(0, add)
>>> rdd3.keyBy(lambda x: x*x)
>>> rdd.cartesian(rdd2).collect()
```

Aggregate RDD elements of each partition, and then the results
Aggregate values of each RDD key
Aggregate the elements of each partition, and then the results
Merge the values for each key
Create tuples of RDD elements by applying a function

Mathematical Operations

```
>>> rdd.subtract(rdd2)
>>> rdd2.subtractByKey(rdd)
>>> rdd.cartesian(rdd2).collect()
```

Return each rdd value not contained in rdd2
Return each (key,value) pair of rdd2 with no matching key in rdd
Return the Cartesian product of rdd and rdd2

Sort

```
>>> rdd2.sortBy(lambda x: x[1])
>>> rdd2.sortBy(lambda x: x[1], ('a',2))
>>> rdd2.sortBy(lambda x: x[1], ('a',2))
>>> rdd.cartesian(rdd2).collect()
```

Sort RDD by given function
Sort (key, value) RDD by key

Repartitioning

```
>>> rdd.repartition(4)
>>> rdd.coalesce(1)
```

New RDD with 4 partitions
Decrease the number of partitions in the RDD to 1

Saving

```
>>> rdd.saveAsTextFile("rdd.txt")
>>> rdd.saveAsHadoopFile("hdfs://namenodehost/parent/child", org.apache.hadoop.mapred.TextOutputFormat)
```

Stopping SparkContext

```
>>> sc.stop()
```

Execution

```
$ ./bin/spark-submit examples/src/main/python/pi.py
```

DataCamp

Learn Python for Data Science Interactively



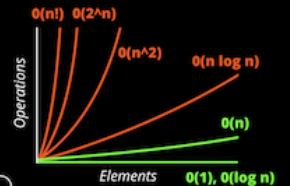
LEGEND

TIME Complexity vs. SPACE Complexity



<BIG-O-CHEATSHEET>

www.bigocheatsheet.com



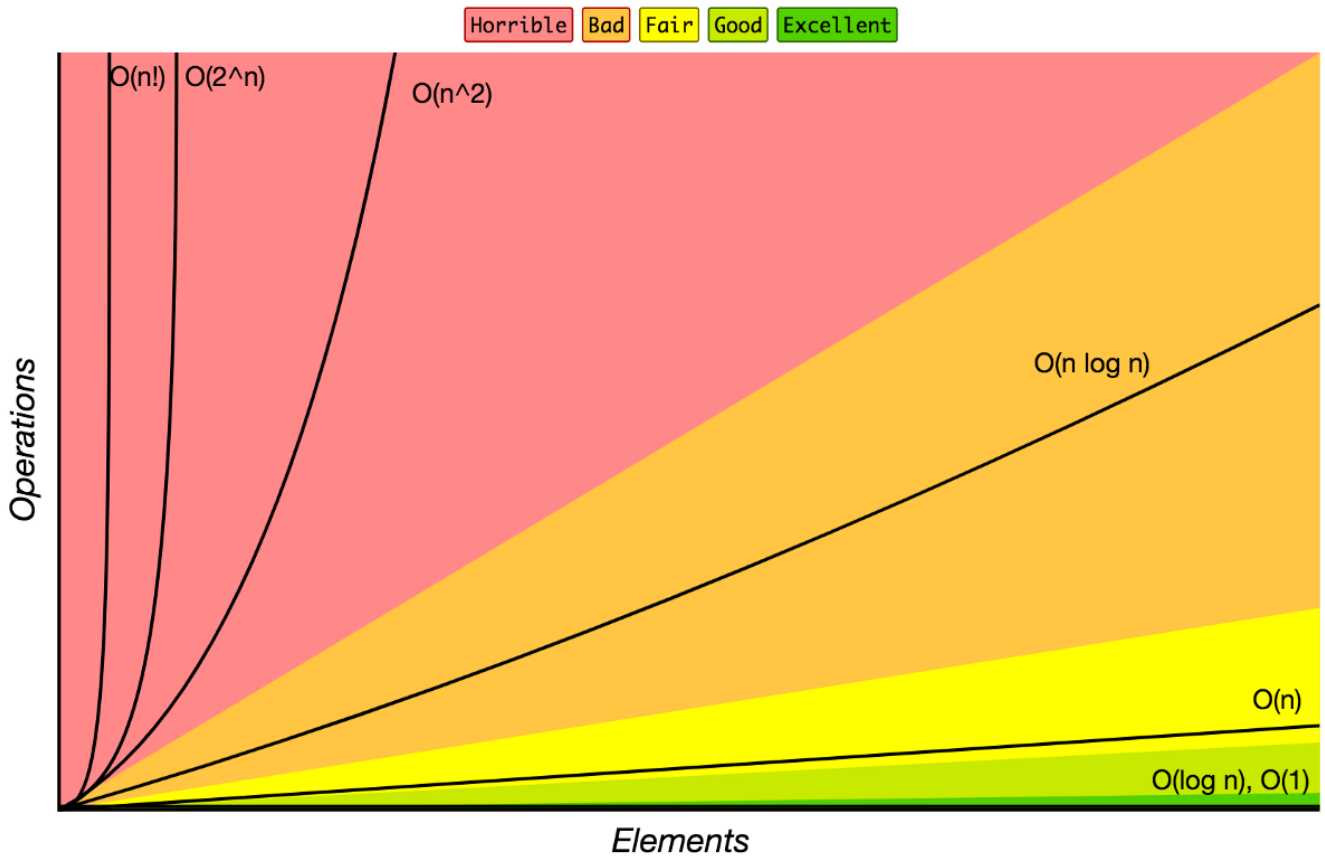
DATA STRUCTURE Operations

| DATA Structure | TIME Complexity | | | | SPACE Complexity | | | |
|--------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|---------------------|
| | Access | Search | Insertion | Deletion | Access | Search | Insertion | Deletion |
| Array | $\Theta(1)$ | $\Theta(n)$ | $\Theta(n)$ | $\Theta(n)$ | $\Theta(1)$ | $\Theta(n)$ | $\Theta(n)$ | $\Theta(n)$ |
| Stack | $\Theta(n)$ | $\Theta(n)$ | $\Theta(1)$ | $\Theta(1)$ | $\Theta(n)$ | $\Theta(n)$ | $\Theta(1)$ | $\Theta(1)$ |
| Queue | $\Theta(n)$ | $\Theta(n)$ | $\Theta(1)$ | $\Theta(1)$ | $\Theta(n)$ | $\Theta(n)$ | $\Theta(1)$ | $\Theta(1)$ |
| Singly-Linked List | $\Theta(n)$ | $\Theta(n)$ | $\Theta(1)$ | $\Theta(1)$ | $\Theta(n)$ | $\Theta(n)$ | $\Theta(1)$ | $\Theta(1)$ |
| Doubly-Linked List | $\Theta(n)$ | $\Theta(n)$ | $\Theta(1)$ | $\Theta(1)$ | $\Theta(n)$ | $\Theta(n)$ | $\Theta(1)$ | $\Theta(1)$ |
| Skip List | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(n)$ | $\Theta(n)$ | $\Theta(n)$ | $\Theta(n \log(n))$ |
| Hash Table | N/A | $\Theta(1)$ | $\Theta(1)$ | $\Theta(1)$ | N/A | $\Theta(n)$ | $\Theta(n)$ | $\Theta(n)$ |
| Binary Search Tree | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(n)$ | $\Theta(n)$ | $\Theta(n)$ | $\Theta(n)$ |
| Cartesian Tree | N/A | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | N/A | $\Theta(n)$ | $\Theta(n)$ | $\Theta(n)$ |
| B-Tree | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ |
| Red-Black Tree | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ |
| Splay Tree | N/A | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | N/A | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ |
| AVL Tree | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ |
| KD Tree | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(\log(n))$ | $\Theta(n)$ | $\Theta(n)$ | $\Theta(n)$ | $\Theta(n)$ |

ARRAY SORTING Algorithms

| ARRAY Algorithms | TIME Complexity | | | SPACE Complexity | |
|------------------|---------------------|------------------------|------------------------|------------------|-------------------|
| | Best | Average | Worst | Worst | Worst |
| Quicksort | $\Omega(n \log(n))$ | $\Theta(n \log(n))$ | $\Theta(n^2)$ | $\Theta(n)$ | $\Theta(\log(n))$ |
| Mergesort | $\Omega(n \log(n))$ | $\Theta(n \log(n))$ | $\Theta(n \log(n))$ | $\Theta(n)$ | $\Theta(n)$ |
| Timsort | $\Omega(n)$ | $\Theta(n \log(n))$ | $\Theta(n \log(n))$ | $\Theta(n)$ | $\Theta(1)$ |
| Heapsort | $\Omega(n \log(n))$ | $\Theta(n \log(n))$ | $\Theta(n \log(n))$ | $\Theta(n)$ | $\Theta(1)$ |
| Bubble Sort | $\Omega(n)$ | $\Theta(n^2)$ | $\Theta(n^2)$ | $\Theta(n)$ | $\Theta(1)$ |
| Insertion Sort | $\Omega(n)$ | $\Theta(n^2)$ | $\Theta(n^2)$ | $\Theta(n)$ | $\Theta(1)$ |
| Selection Sort | $\Omega(n^2)$ | $\Theta(n^2)$ | $\Theta(n^2)$ | $\Theta(n)$ | $\Theta(1)$ |
| Tree Sort | $\Omega(n \log(n))$ | $\Theta(n \log(n))$ | $\Theta(n^2)$ | $\Theta(n)$ | $\Theta(n)$ |
| Shell Sort | $\Omega(n \log(n))$ | $\Theta(n(\log(n))^2)$ | $\Theta(n(\log(n))^2)$ | $\Theta(1)$ | $\Theta(1)$ |
| Bucket Sort | $\Omega(n+k)$ | $\Theta(n+k)$ | $\Theta(n^2)$ | $\Theta(n)$ | $\Theta(n)$ |
| Radix Sort | $\Omega(nk)$ | $\Theta(nk)$ | $\Theta(nk)$ | $\Theta(n+k)$ | $\Theta(n+k)$ |
| Counting Sort | $\Omega(n+k)$ | $\Theta(n+k)$ | $\Theta(n+k)$ | $\Theta(n+k)$ | $\Theta(k)$ |
| Cubesort | $\Omega(n)$ | $\Theta(n \log(n))$ | $\Theta(n \log(n))$ | $\Theta(n)$ | $\Theta(n)$ |

Big-O Complexity Chart



Common Data Structure Operations

| Data Structure | Time Complexity | | | | | | | | Space Complexity |
|--------------------|-------------------|-------------------|-------------------|-------------------|--------------|--------------|--------------|--------------|------------------|
| | Average | | | | Worst | | | | Worst |
| | Access | Search | Insertion | Deletion | Access | Search | Insertion | Deletion | |
| Array | $O(1)$ | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ | $O(1)$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ |
| Stack | $\theta(n)$ | $\theta(n)$ | $\theta(1)$ | $\theta(1)$ | $O(n)$ | $O(n)$ | $O(1)$ | $O(1)$ | $O(n)$ |
| Queue | $\theta(n)$ | $\theta(n)$ | $\theta(1)$ | $\theta(1)$ | $O(n)$ | $O(n)$ | $O(1)$ | $O(1)$ | $O(n)$ |
| Singly-Linked List | $\theta(n)$ | $\theta(n)$ | $\theta(1)$ | $\theta(1)$ | $O(n)$ | $O(n)$ | $O(1)$ | $O(1)$ | $O(n)$ |
| Doubly-Linked List | $\theta(n)$ | $\theta(n)$ | $\theta(1)$ | $\theta(1)$ | $O(n)$ | $O(n)$ | $O(1)$ | $O(1)$ | $O(n)$ |
| Skip List | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(n \log(n))$ |
| Hash Table | N/A | $\theta(1)$ | $\theta(1)$ | $\theta(1)$ | N/A | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ |
| Binary Search Tree | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ |
| Cartesian Tree | N/A | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | N/A | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ |
| B-Tree | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$ |
| Red-Black Tree | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$ |
| Splay Tree | N/A | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | N/A | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$ |
| AVL Tree | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$ |
| KD Tree | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ |

Array Sorting Algorithms

| Algorithm | Time Complexity | | | Space Complexity |
|-----------------------|---------------------|------------------------|-------------------|------------------|
| | Best | Average | Worst | Worst |
| <u>Quicksort</u> | $\Omega(n \log(n))$ | $\theta(n \log(n))$ | $O(n^2)$ | $O(\log(n))$ |
| <u>Mergesort</u> | $\Omega(n \log(n))$ | $\theta(n \log(n))$ | $O(n \log(n))$ | $O(n)$ |
| <u>Timsort</u> | $\Omega(n)$ | $\theta(n \log(n))$ | $O(n \log(n))$ | $O(n)$ |
| <u>Heapsort</u> | $\Omega(n \log(n))$ | $\theta(n \log(n))$ | $O(n \log(n))$ | $O(1)$ |
| <u>Bubble Sort</u> | $\Omega(n)$ | $\theta(n^2)$ | $O(n^2)$ | $O(1)$ |
| <u>Insertion Sort</u> | $\Omega(n)$ | $\theta(n^2)$ | $O(n^2)$ | $O(1)$ |
| <u>Selection Sort</u> | $\Omega(n^2)$ | $\theta(n^2)$ | $O(n^2)$ | $O(1)$ |
| <u>Tree Sort</u> | $\Omega(n \log(n))$ | $\theta(n \log(n))$ | $O(n^2)$ | $O(n)$ |
| <u>Shell Sort</u> | $\Omega(n \log(n))$ | $\theta(n(\log(n))^2)$ | $O(n(\log(n))^2)$ | $O(1)$ |
| <u>Bucket Sort</u> | $\Omega(n+k)$ | $\theta(n+k)$ | $O(n^2)$ | $O(n)$ |
| <u>Radix Sort</u> | $\Omega(nk)$ | $\theta(nk)$ | $O(nk)$ | $O(n+k)$ |
| <u>Counting Sort</u> | $\Omega(n+k)$ | $\theta(n+k)$ | $O(n+k)$ | $O(k)$ |
| <u>Cubesort</u> | $\Omega(n)$ | $\theta(n \log(n))$ | $O(n \log(n))$ | $O(n)$ |